Suggestion that recent (≤ 3 Ga) flux of kilometer and larger impactors in the Earth-Moon system has not been constant

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ABSTRACT

Lunar impact crater chronologies have been developed by combining carefully measured crater densities of lunar terrains with radiometric ages provided by returned samples. However, due to the sparse coverage of the samples during the last three billion years, this part of the chronologies is not well constrained. Lunar crater chronologies generally assume that the bombardment rate has been relatively constant during this epoch for all impactor sizes. Nevertheless, evidence has been gathering that this may not be the case for impactors larger than several hundred meters; however, there may be biases related to some of this evidence. The break-up of large asteroids in the Main Asteroid Belt to make asteroid families could be a source of a changing impact flux in the Earth-Moon system, especially when the families form near strong orbital resonances with the gas giants. In order to further explore the state of the impact flux from today to three billion years ago for impactors larger than ~5 km, we calculate crater retention model ages of 43 lunar craters 50 km and larger in diameter (D). Selected craters were initially suggested by United States Geological Survey geological maps of the Moon and Wilhems (1987) to have formed during the Copernican and Eratosthenian. We use the density of small (D < a few km) craters superposed on their floors, along with Model Production Function (MPF) lunar chronology (Marchi et al., 2009). For this purpose, we assume that the smaller impactors forming the superposed craters follow a constant flux as indicated by the MPF and supported by models of the dynamical evolution of the impactor population. We use the model ages as a proxy for the impact flux of larger impactors and test whether their distribution in time is consistent with a constant flux using two statistical analyses. Our results suggest that the flux of these larger impactors could be variable during the last three billion years, with hints of a relative increase in flux occurring ~2 billion years ago and a decrease in flux ~1 billion years ago. Thus, our results support the evidence that the impact flux has varied on the Moon for impactors over a few kilometers in diameter.

1. Introduction

Absolute cratering chronologies for the Moon have been developed as a outcome of human and robotic sample return missions (e.g., Hartmann et al., 1981; Le Feuvre and Wieczorek, 2011; Marchi et al., 2009; Neukum et al., 2001; Neukum and Ivanov, 1994; Robbins, 2014). These chronologies pair the crater spatial densities from known regions to the radiometric ages of the returned samples (e.g., Stöffler et al., 2006; Stöffler and Ryder, 2001). The problem is that because locations and samples are limited, there are still many unknowns about the chronology, especially in recent epochs, from about three billion years ago until today. In general, the published lunar chronologies assume that the flux has been relatively constant during this time period for all impactors regardless of size. Evidence has been developing, however, that this may not be the case.

Relative increases in crater production for relatively short time periods of about a few hundred million years (“spikes”) in the last few billion years for the Earth-Moon system have been noticed in a variety of data sets. We start by listing this evidence, then discuss the issues.

First, potential spikes in the production of lunar impact glasses have been observed in various Apollo samples at ~0.5, 0.8, 1.5, and 2.5 Ga (Culler et al., 2000; Hui et al., 2009; Levine et al., 2005; Muller et al., 2001; Norman et al., 2012; Zellner et al., 2009; Zellner and Delano, 2015). Second, similar spikes are indicated by the increased number of L-chondrite fossilized meteorites found on Earth at ~0.5 and 0.8 Ga (Schmitz et al., 2003). Third, the radiometric ages of craters on Earth may show evidence for an increase in the flux within the last few hundreds of millions of years and a potential increase around 2 Ga (Grieve, 2001).
100 km craters are expected from the family than the background. This would result in a ‘spike’ in the background source of impactors. Note that fewer D impacts from smaller to larger impactors going left to right. Using simple scaling (x10; Marchi et al. (2009)) the approximate crater diameter (D) formed on the Moon is also shown. Based upon these simulation results Bottke et al. (2007) predict the number of impacts shown for each impactor diameter from the family and Fig. 1.

On the “con” side, we caution that recent works have argued that the young spikes indicated by Apollo glasses could be due to thermal strain breaking up glasses (Zellner and Delano, 2015) and/or sampling and other biases (Huang et al., 2015; Hui et al., 2009). Optical maturity studies of lunar rayed craters also counter-indicate an increase of impact flux at 800 Ma (Grier et al., 2001; Grier and McEwen, 2001). Finally, work by Guinness and Arvidson (1977) argued for a constant flux for craters between 0.1 and 1 km in diameter over the last 3.3 Ga given the similarity in the crater size-frequency distribution shapes for terrains examined in this time frame.

Short or long-term relative decreases from average in the impact flux (“lulls”) in the last few billion years have also been potentially indicated. One such lull was suggested by Mazrouei et al. (2019), who argued from their lunar crater ages that the impact flux was distinctly lower between ~300–1000 Ma. They argued that a lower impact flux is also seen in terrestrial craters formed on cratons between 300 and 650 Ma. Others believe this terrestrial crater deficit might be a result of erosion and crater degradation (see Grieve, 1984), though this would not explain the relatively intact nature of kimberlite pipes found in the same locations as terrestrial craters (see also Keller et al., 2019). Long-term lulls (or declines in the impact rate since ~3 Ga) have been suggested based upon slower than expected crater degradation rates (Craddock and Howard, 2000), along with ages of lunar impact melts (in lunar meteorites) and lunar glasses (excluding the indicated spikes discussed above) (Hartmann et al., 2007). A long-term lull between 1 and 2 Ga was also indicated for Mars using superposed crater densities on larger craters by Lagain et al. (2020).

Observations and simulations have shown that the break-up of large asteroids by impacts to produce families is not uncommon (Bottke et al., 2007; Gladman et al., 1997; Masiero et al., 2015; Nesvorný et al., 2002, 2015; Vokrouhlík et al., 2017; Zappalà et al., 1998). Observations of the dynamical properties of the families can provide the approximate time of their formation (Bottke et al., 2006; Nesvorný et al., 2002, 2015). Furthermore, simulations have shown when these break-ups occur near resonances they can become sources for increased delivery of objects to impact the Earth-Moon system (e.g., Bottke et al., 2007; Vokrouhlík et al., 2017; Fig. 1). Observations of impact events timing for the parent bodies of meteorites support this idea (e.g., Nesvorný et al., 2009).

So far the size of impactors involved in the possible observed spikes or lulls and produced by the asteroid break-ups has not been specified. The observations discussed above potentially cover a wide range of impactor sizes from meters (fossil meteorites and impact glasses) to several tens of kilometers (large craters and impact melts). Thus, increases or decreases in the number of impactors created and delivered to the Earth-Moon system could be occurring at a wide range of sizes at different times or i.e., the size-frequency distribution of the impactors changes shape, if all observations are accepted equally. Furthermore, simulations indicate the rate of increased delivery over the background rate is potentially different for different impactor sizes. Small impactors, less than a few hundred meters or so, do not appear to increase much over their background except for very short time periods (Guinness and Arvidson, 1977; Nesvorný et al., 2009), while larger impactors, appear to show increases lasting a few hundreds of millions of years over the background flux at these sizes (Bottke et al., 2007; Mazrouei et al., 2019; Fig. 1). This would imply that at certain sizes we would see an increase

Fig. 1. Simulation results of impacts in the Earth-Moon system from the Baptistina asteroid family (BAF) by Bottke et al. (2007). Each panel is for a different sized impactor (d) from smaller to larger impactors going left to right. Using simple scaling (x10; Marchi et al. (2009)) the approximate crater diameter (D) formed on the Moon is also shown. Based upon these simulation results Bottke et al. (2007) predict the number of impacts shown for each impactor diameter from the family and the background source of impactors. Note that fewer D > −10 km craters are expected from the family than from the background impactors, while more D > −50 and 100 km craters are expected from the family than the background. This would result in a ‘spike’ in impacts over an ~100 Myr timespan for larger craters, while D < −10 km would remain relatively constant. Figure modified from Bottke et al. (2007).
in crater production on the Earth and Moon at certain times.

We use modern versions of the techniques used by Baldwin and McEwen to derive the absolute crater model ages and flux of large lunar craters. We measure small craters (D \sim 0.01–5 km, likely made by projectiles that are sub-meter to a few hundred meters) superposed on their floors, since floors appear to provide a more reliable estimation of the crater distribution than counts on the ejecta blankets for the Moon (Plescia, 2012; Plescia and Robinson, 2011; Zanetti et al., 2017). Then, we use the Model Production Function (MPF; Marchi et al., 2009) lunar chronology to fit the crater size-frequency distributions and derived absolute model ages of the large craters. We assume that the flux of the smaller and larger craters are disconnected, with the small craters having the constant flux as expected by the MPF (see Guinness and Arvidson, 1977 and supplemental materials in Mazrouei et al., 2019). As described above, this may be theoretically expected if asteroid families are the cause of changes in flux, as simulations indicate that the large impactors from families do increase above background, while the small ones do not (Bottke et al., 2007; Fig. 1). In Section 2, we present our methods, including discussion of the sources of uncertainties in the absolute model ages, such as secondary craters. In Section 3, we present the ages and statistical analyses of the implied flux. Finally, in Section 4, we discuss the implications for any observed variations from a constant flux and comparisons with known families and other data sets indicating variability in the flux.

2. Methods

Because we are interested in the crater flux during the Copernican and Eratosthenian eras (~0–3.2 Ga; Stöffler and Ryder, 2001), we analyze craters initially identified as potentially forming in those epochs by the United States Geological Survey (USGS) geological maps of the Moon from the 1970s (e.g., Wilhelms and McCauley, 1971) and/or Wilhelms (1987). These researchers typically used the morphology of the craters to determine which era they formed in, such as occurrence and brightness of ejecta and erosional state of the crater rim and peak; and they did not always agree. For example, we have a few craters labeled by the USGS maps as forming in the L. Imbrian (Fabricius, Leuschner, and Werner; see our Table 2), as Wilhelms identified them as forming in the Eratosthenian (see Supplemental Material). We note that by not including all craters labeled as formed in the Imbrian by both these earlier data sets, we may have missed some craters that could have crater retention model ages consistent with possible formation in the Copernican or Eratosthenian. However, we expect this number to be low, as typically our crater retention model ages indicate the same epoch or older, instead of younger ages (Table 2). In fact, we only observe one crater with a crater retention model age less than its morphological age as determined by either earlier classification (Ohm, Table 2). Furthermore, in our earlier study (Kirchoff et al., 2013), where we included some initially labeled Imbrian craters, we found none of these were younger than their initially predicted ages. Thus, given a maximum rate of ~2% that could be younger using our methods, we would only expect to get a minimum age for these craters and then assumed the maximum age is the maximum for the Eratosthenian (3.2 Ga). For Tsiolkovskiy, density of smaller craters superposed on their floors (which we abbreviate SSC for small, superposed craters) (e.g., Fig. 3). We use both the LROC Wide Angle Camera (WAC) global mosaic at a pixel scale of 100 m/pixel at the equator and LROC Narrow Angle Camera (NAC) images at pixel scales of 0.5–1 m/pixel. The NAC images are primarily needed for smaller and younger craters to obtain enough SSCs to reduce uncertainties on the crater distributions. We use JMARS (http://jmars.asu.edu/) to view the WAC global mosaic and find NAC images where needed.

There are two craters – Hercules and Tsiolkovskiy – which have had their floors covered by maria, making it difficult to include them using our methods. We considered instead counting their ejecta blankets, but this would introduce a difference in ages due to differing terrain properties (e.g., Kirchoff and Marchi, 2019; Marchi et al., 2011; van der Bogert et al., 2017). This could be theoretically corrected for using the MPF (e.g., Marchi et al., 2009); however, the correction to use to get the most reliable age is uncertain (e.g., Kirchoff and Marchi, 2019). Therefore, we decided not to introduce this additional uncertainty using a different methodology. Nevertheless, we did want to understand the effect of including these craters, so we measured superposed craters on the mare (which should have similar material properties to crater floors) to get a minimum age for these craters and then assumed the maximum age is the maximum for the Eratosthenian (3.2 Ga). For Tsiolkovskiy,
there may be small areas of the original floor left (see Supplemental Fig. S40), so we measured superposed craters on these as well to get additional constraints on this crater’s formation age.

We use the JMARS 3-point crater tool to measure SSCs once identified. This tool provides the diameter of the SSC, along with its center latitude and longitude. We also classify the SSCs with a degradation state (e.g., Fig. S40), so we measured superposed craters on these as well to get additional constraints on this crater’s formation age.

Differential, and relative (R) formats (Crat. Anal. Tech. Work. Group, 1979) as they each have something unique to offer for the analyses. The cumulative, differential and relative techniques use a kernel density estimator (KDE) to compute the crater size-frequency distributions (SFDs). We use the cumulative, differential, and relative (R) formats (Crat. Anal. Tech. Work. Group, 1979) as they each have something unique to offer for the analyses. The cumulative distribution is used to derive the relative and absolute model ages of the large craters (e.g., Figs. 3, 4). Degradation state is on a scale of 1–4 with 1 representing the freshest craters with sharp rims, deep cavities, and no visible superposed craters (e.g., Fig. 3, red circles). Classes 2 and 3 have more eroded rims and cavities that are partially filled (e.g., yellow and green circles, respectively in Fig. 3), with Class 2 craters having sharper rims and deeper bowls than Class 3. Class 4 craters are the most eroded, sometimes with no identifiable rim and little depth (e.g., Fig. 3, blue circles). Crater depth is subjectively determined by shadows. Secondary craters are those that form from the fast, blocky ejecta of a larger primary crater. Obvious secondary craters (OSCs) then are defined here as those secondary craters that form in chains and clusters, and may have a distinctive herringbone pattern (e.g., Oberbeck and Morrison, 1974). We do not classify lone elliptical craters as OSCs as they may be elliptical primaries. For further details on classifications see Kirchoff et al. (2013).

We use the JMARS 3-point crater tool to measure SSCs once identified. This tool provides the diameter of the SSC, along with its center latitude and longitude. We also classify the SSCs with a degradation state (e.g., Fig. S40), so we measured superposed craters on these as well to get additional constraints on this crater’s formation age.

Once we have compiled the SSCs for each large crater, we analyze the SSC size-frequency distributions (SFDs). We use the cumulative, differential, and relative (R) formats (Crat. Anal. Tech. Work. Group, 1979) as they each have something unique to offer for the analyses. The cumulative distribution is used to derive the relative and absolute model ages of the large craters (e.g., Figs. 3, 4). The differential distribution is used to compare the presumed primary SSC SFD with the crater SFD for the OSCs, along with computing the differential slope for the SSC and OSC SFDs (e.g., Fig. 4). The R-plot is used to compare how the various crater degradation classes contribute to the SSC SFD and the overall shape of the SSC SFD (e.g., Fig. 4).

We use the new, more statistically robust techniques described in Robbins et al. (2018) to compute all SSC SFDs (e.g., Figs. 3, 4). These techniques use a kernel density estimator (KDE) to compute the crater SFDs and bootstrap to compute the associated uncertainties. We also use the recommended minimum likelihood estimator (MLE) technique for computing the differential slope. The advantages of these techniques is that they include more uncertainties associated with crater measurements than traditional techniques. First, the KDE allows us to include the uncertainty on the diameter measurement into the SFD (Robbins et al., 2018). Second, bootstrap uncertainties are derived directly from the data without the need to assume a structure to the data that may not be correct (e.g., Poisson). They have also been expanded to represent the 99th percentile (equivalent to 3σ for a Gaussian; in the differential and cumulative plots the traditional 2σ equivalents are also shown by the lighter lines within the shaded areas), thus potentially incorporating more sources of error. Finally, MLE also relies directly on the data rather than assuming it has a structure and has less error and restrictions (e.g., requiring a certain number of points) associated with the fit to the data. We show traditional versions of each of the cumulative crater SFDs represented by squares with error bars to demonstrate that the new technique corresponds to traditional ones well while providing more statistically robust information. Plots similar to Fig. 4 are given for all craters in Supplementary Material (excluding representation of traditional techniques).

Absolute ages and their uncertainties are estimated using the Model Production Function for the Moon (MPF; Marchi et al., 2009) to a precision of 0.1 Ga (e.g., Fig. 3; we suggest this is the minimum precision for any lunar crater chronology; see e.g., Kirchoff et al., 2013). This chronology is able to incorporate the different distributions for both Near Earth Objects (NEO) and Main Belt Asteroids, along with the effect of terrain strength on the formation of craters with diameters less than about a few hundred meters, when computing the shape of the crater production function. Based upon our preliminary understanding of relevant impactors, terrain properties, and sizes of SSCs (D > 10 m), we start with using the distribution for NEOs and the gravity-regime scaling law for competent rock from Melosh (1989); eqs. 7.8.4, target density = 2.8 g/cm³, projectile density = 2.6 g/cm³, and impact velocity distribution from fig. 1 in Marchi et al., 2009; converted to final diameters using standard relationships and simple-to-complex transition diameter of 18 km, e.g., Marchi et al., 2009). We find that this production function

Fig. 2. Locations of study craters as indicated by colored circles. Numbers correspond to the numbers given in Table 1. Sizes are indicated by the colors with red for D ≥ 100 km, orange for D = 90–99 km, yellow for D = 80–89 km, green for D = 70–79 km, blue for D = 60–69 km, and purple for D = 50–59 km. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
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Fig. 3. Examples of crater measurements, cumulative SFDs, and fitting with the MPF. Left column shows the crater measurements and NAC images, if used, superposed on the WAC mosaic. Colored circles represent the SSCs measured and their classification. Red are class 1 craters, yellow for class 2, green for class 3, and blue for class 4. Pink circles denote the OSCs. Right column shows the cumulative SSC SFDs in both the new KDE format (black/gray lines and shaded areas) and traditional binned format (black squares and error bars). The solid cyan line is the best MPF to the data and the computed age is indicated in the upper right. The vertical, dashed black line indicates the completeness diameter (below which data are incomplete) and small vertical lines at bottom of plot indicate diameter of each SSC (i.e., rug plot). (a) Aristoteles. Example of data fit well by the MPF for small craters, but not large. (b) Cavalerius. Data only collected from WAC mosaic, so data are reduced; however, SFD is fit well by the MPF. (c) Leuschner. Example of data fit well by the MPF over complete diameter range. (d) Werner. Example of large craters fit well by the MPF, but not small. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

generally fits our data well, and thus have not explored other possible production functions with different scaling laws. However, there is some variation in the fits as shown in Fig. 3. For Aristillus and Leuschner we see examples of “good” fits to data gathered from NAC images. A “good” qualitative assessment implies most or all of the cumulative crater SFD was fit well by the MPF. The SFD for Aristillus does not have a perfect fit because the SFD of the larger craters has a more shallow slope than the MPF. This “v-shape” (called such due to its appearance in a R-plot) has been observed before (Hartmann, 1995; Kirchoff et al., 2013) and may be a characteristic of the impactor population, but it is more likely here due to poor statistics for these largest SSCs in a small count area (e.g., Warner et al., 2015). For Cavalerius and Werner, we see examples of “adequate” fits to data. The qualitative definition of an “adequate” fit is that either part of the SSC SFD was fit well, but another part is not (e.g., Werner), or that there are fewer points that are fit well (e.g., Cavalerius). Cavalerius superposed counts are only compiled from the WAC mosaic (SSC diameters are restricted to be ≥500 m to assure completeness). Due to the low density of craters, there are not many data points to fit and uncertainties are large; nevertheless, the MPF actually fits the few data points well. For some of the large craters, however, this was not the case and data only from the WAC mosaic resulted in a poor fit (e.g., D ≥ 500 m craters for Aristillus in Fig. 3). Thus, for these we used NAC images to expand the SSC SFDs to smaller diameters to see if the fit could be improved. This helped improve the fits and estimated absolute model ages for several craters, as exemplified with Aristillus (Fig. 3; see also Supplemental Fig. S2). However, we also observed some cases where the additional data did not help, such as Werner (Fig. 3). This is because the shape (or slope) of small lunar craters with diameters less than a couple hundred meters can vary due to several reasons (for additional review see Williams et al., 2017): 1) erosion of small craters (e.g., Fassett and Thomson, 2014), 2) crater saturation (e.g., Hirabayashi et al., 2017), 3) unrecognized, isolated secondaries (e.g., Bierhaus et al., 2018), and/or 4) effect of craters forming in the strength regime (e.g., Marchi et al., 2009). Reason #4 is not likely for most of our SSC SFDs because this effect does not cause such a dramatic change in slope – the turnover is usually more subtle (Kirchoff and Marchi, 2019; Marchi et al., 2009). Therefore, it is likely due to either all or one of the other reasons, and this part of the SFD should not be fit as we have done for Werner (Fig. 3) and other SSC SFDs affected in this way (Supplemental Figs. S9, S31, S35).

Once absolute model ages are computed, we use the large crater morphology to determine if the ages are likely formation ages of these craters. In general, the relative youth of these craters and their generally preserved morphologies indicate we are likely obtaining their formation ages with the SSCs observed on their floors (i.e., the floors have not been significantly resurfaced). The exceptions are Hercules and Tsiolevskiy, which have their floors apparently covered by mare. As we have discussed above, we have estimated minimum and maximum ages for these craters with the formation age likely somewhere in between. The formation ages can then be used as a proxy for impact flux for these sized craters and associated impactor sizes (roughly 2–10 km).

To determine if the impact flux has been constant or variable in the last 3 Ga for these sized impactors, we use two Monte Carlo-type analyses to determine how frequently the observed distribution of craters’ ages would occur for a constant flux. First, we draw ages for 0.1 Ga intervals to correspond to our model age precision for the number of craters observed for each diameter range (≥100 km, ≥90 km, ≥80 km, ≥70 km, ≥60 km, and ≥ 50 km) only with ages <3 Ga (e.g., 3 Ga, or 10 Ga). Next, we create 100 individual summed kernel density functions (a.k.a., an ideogram), where the kernel has a Gaussian shape centered at the age
and a width derived from the randomly selected uncertainty (uses the norm function from the Python SciPy package). We also create an ideogram for the observed ages and their uncertainties computed from the MPF fit to the data for each diameter range (see e.g., Fig. 6, dashed gray lines; while we use published radiometric ages for Copernicus and Tycho, we continue to use our 0.1 Ga minimum uncertainty for these tests). Using these continuous functions, we can perform a Kolmogorov-Smirnov test \( (K-S\) test; e.g., Wall and Jenkins, 2003) to determine if the observed data and drawn data come from the same (constant) distribution. If we observe any distributions for a diameter range that are different at a \( \geq 95\% \) significance level, then we conclude the observed distribution of ages with their uncertainties is not likely derived from a constant flux. Note that due to the small numbers of craters, the distribution of \( D \geq 100 \) and 90 craters could not be tested with this technique.

Second, to test the distributions with few ages less than 3 Ga (\( D \geq 90 \) and 100 km), and determine when and what type of deviation from constant flux may have occurred, we modify the first analysis above. We now randomly draw crater ages with a precision of 0.1 Ga from the full MPF lunar chronology (Marchi et al., 2009), which assumes a constant flux from now until 3 Ga and then exponential for \( >3 \) Ga. However, we have modified the exponential to decrease to zero craters by 4 Ga (Fig. 5). This modification is done for two reasons: 1) our interest is for craters that have formed from \( \leq 3 \) Ga, so we do not expect to analyze many craters older than \( \sim 3.8 \) Ga, and 2) SSCs less than a kilometer or so

Fig. 4. Example of generating and analyses of the different crater SFD formats. Solid lines with shaded areas represent the KDE and bootstrap versions of the crater SFDs and their uncertainties. Squares and error bars represent the traditional version of the cumulative crater SFD and its uncertainty for comparison. Left plot: differential crater SFDs of all SSCs excluding OSCs (black/gray) and OSCs (pink), along with computed slopes in brown and tan respectively. Upper right plot: cumulative crater SFD of all SSCs excluding OSCs with best MPF fit (cyan line) and computed model age. Lower right plot: relative crater SFDs of all SSCs excluding OSCs (black/gray), class 1 SSCs (red), class 2 SSCs (yellow), class 3 SSCs (green), and class 4 SSCs (blue). In all plots the vertical dashed line indicates the completeness diameter with value given in the relative plot along with other information related to computing the KDE and bootstrap uncertainties. All plots also display a “rug plot” of the crater diameters measured (small vertical lines at bottom of plots). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
are erased for surfaces older than ~3.8 Ga, therefore, we would not expect our ages to be accurate beyond this point (e.g., Fassett and Thomson, 2014). The histogram of our estimated ages using 0.1 Ga bins (see Section 3 for reasoning) in Fig. 5 shows that this is indeed the case and verifies our modified chronology. A draw is done 100 times for each observed distribution of ages we analyze (e.g., five crater ages are drawn 100 times for D ≥ 100 km craters). The results of the 100 individual tests are then compared to the observed distribution of ages for only ≤ 3 Ga to determine how many times that distribution is observed for a constant distribution. We again assume all sizes have an equal probability of forming. If an observed age distribution is frequently selected (> 5% of the time), we conclude it is consistent with a constant flux. However, if an observed age distribution is infrequently selected (< 1% of the time), we conclude it is plausibly not consistent with a constant flux (similar to ≥ 5% of the time then we suggest it is plausibly not consistent with a constant flux (similar to ≥ 3σ significance reported for Gaussian distributions). Values in between 1 and 5% are considered possibly not consistent with a constant flux (similar to ≥ 2σ significance reported for Gaussian distributions). The disadvantage of this analysis is that age uncertainties can no longer be included. However, we only test for deviations in distributions already indicated to not likely be constant by the first analysis that incorporates uncertainties. Furthermore, although this is the only test for D ≥ 100 km craters, uncertainties play a minor to no role since these have so few craters with ages ≤ 3 Ga.

### 3. Results

Table 2 presents the absolute model formation age, related Stoffler epoch, original USGS epoch, relative age (observed cumulative density at D ≥ 1 km), differential slope of the SSC SFD, and qualitative assessment of the MPF fit to the SSC SFD (see Fig. 3 for examples of fit qualities). Craters are listed by diameter group with largest first (see Table 1 for diameters), then by age. Fig. 6 presents histograms of the model ages using 0.1 Ga bins, along with the summed kernel (Gaussian) density functions of the model ages and their uncertainties (dashed lines) for each diameter range. Other larger bin sizes (it would not make sense to use bin sizes smaller than our precision) were not explicitly tested, because the first Monte Carlo-type analysis using the summed kernel density functions implicitly tested this by incorporating the uncertainties on the ages, which would also be the purpose of using larger bins.

The K–S test results from the first Monte Carlo-type analysis of the distributions of crater formation ages and their uncertainties for diameter ranges testable with this technique (D ≥ 50, 60, 70, and 80 km) indicate that the D ≥ 50 km distribution is the only one that is significantly different (≥ 95%) from a constant flux (Fig. 6f, gray dashed line). The D ≥ 80, 70 and 60 km distributions could all be derived from a constant flux (Fig. 6c–e, gray dashed lines).

From the second Monte Carlo-type statistical analysis of the ages, which cannot include uncertainties, for the D > 100, 90, and 50 km distributions (Fig. 6a, b, f), we find that there are some plausible (probability ≥ 99%) and possible (probability 95–98%) spikes and/or lulls for each distribution (Table 3). Note that the age ranges given include the endpoints for spikes, while they exclude the endpoints for lulls. In Fig. 6 we visualize some of the more probable spikes (black highlights) and lulls (arrows).

Starting with the D ≥ 100 km group, we find that all four craters with more certain formation ages in that set form before our time period of interest, 3.0 Ga (Fig. 6a). Tsiolkovskiy is likely Eratosthenian in age (0.8–3.2 Ga) based upon its morphology (Greenhagen et al., 2016; Pasckert et al., 2015) and crater density on the edge of the crater floor that does not seem to be resurfaced (N[≤ 1 km] ~ 2500; Supplemental Fig. S40). Furthermore, crater density on the mare that covers the majority of the floor appears to be Eratosthenian in age (2.7 ± 0.2 Ga), implying the crater does not need to be older than Eratosthenian to be covered in mare. Our reported “formation” age of 2.6 ± 0.6 Ga, derived from a synthesis of the data, indicates a wide range of ages to consider for determining the significance of spikes and lulls in the 0–3 Ga time frame. If Tsiolkovskiy is >3 Gyrs, then we find that there is a plausible lull from 0 to 3 Ga with a > 99% probability (Table 3). If Tsiolkovskiy is 2.6 Ga, then we find a possible lull from 0 to 2.6 Ga with a 98% probability (indicated by the arrow in Fig. 6a). If Tsiolkovskiy is our youngest suggested age (2.0 Ga), then the lull is at a 95% probability. Thus, in summary, there appears to be a significant lull in cratering with no craters forming for D ≥ 100 km craters, and the length and significance
of this lull is dependent on the age of Tsiolkovskiy. Continuing with \( D > 90 \) km craters (Fig. 6b), we find that ages are statistically consistent with a constant flux, unless Tsiolkovskiy is \( >3.0 \) Gyrs in age. For an "old" Tsiolkovskiy, we find that there is a possible lull, with no craters forming, between 1.4 and 3.0 Ga (Table 3). The possible lull could be longer from either 0.8–3.0 Ga or 0–3 Ga with some, but fewer than expected, craters forming (Table 3). However, with these results dependent on only one crater of highly uncertain age, we suggest these results are inconclusive.

Finally, for the craters with \( D \geq 50 \) km that have ages \( \leq 3 \) Ga (Fig. 6f), we find multiple probable and possible spikes and lulls (Table 3). This set now includes two craters with uncertain ages – Tsiolkovskiy and Hercules. What is interesting is that their model age estimations vary in similar ways. They both have a span in "best guess" ages from \( \sim 2.0–3.2 \) Ga with a median age \( \sim 2.6 \) Ga (Table 2). We tested six end-member permutations of their ages: the median ages of 2.5 and 2.6 Ga (from Table 2), both \( >3.0 \) Ga, one \( >3.0 \) Ga and one at 2.6 Ga, one \( >3.0 \) Ga and one at 2.0 Ga, one at 2.6 Ga and one at 2.0 Ga, and both at 2.0 Ga. For \( D \geq 50 \) km only in Table 3, we then list only those lulls or spikes that occurred in \( \geq 3 \) permutations and note the number of permutations for each spike or lull. Those with fewer permutations are given in Supplemental Table S2.

The most probable lull in impact flux for \( D > 50 \) km craters occurs between 0.8 and 1.4 Ga (indicated by the arrow in Fig. 6f), but it may possibly be longer (Table 3 and Table S2). A lull in this time span is also indicated by the kernel density function of the ages, which includes the model age’s uncertainties (dashed line in Fig. 6f), supporting that this lull is indeed likely. The most probable spike contains the six craters that occurred in \( >3 \) permutations and note the number of permutations for each spike or lull. Those with fewer permutations are given in Supplemental Table S2.
could be that most of the difference of the kernel density function for the D ≥ 50 km craters from the constant flux indicated by the K–S test (see above) is in the lull and not the spike.

4. Implications for the Recent Flux of Km-sized impactors

The above results suggesting significant lulls and spikes in the crater model formation ages would tend to support – and be supported by – the other evidence for spikes and lulls observed by different data sets (e.g., Craddock and Howard, 2000; Grieve and Shoemaker, 1994; Hartmann et al., 2007; Mazrouei et al., 2019; Muller et al., 2001; Schmitz et al., 2003), and that at least some of that data may not be biased as previously suggested (e.g., Grier and McEwen, 2001; Huang et al., 2018; Zellner and Delano, 2015). Our work and the other analyses seem to imply the number of impacts may have relatively increased for km-sized impactors for roughly a few hundred million years at around 2 Ga. This is most plausibly produced by formation of an asteroid family or families near strong orbital resonances in the Main Asteroid Belt that would push asteroids into the Earth-Moon system (e.g., Bottke et al., 2007; Nesvorný et al., 2015; Vokrouhlický et al., 2017; Fig. 1). Two intriguing families with possible ages near this time (including error bars) that are also near the 3:1 mean motion resonances with Jupiter – a good resonance for delivering material to the Moon – include Maria (Broz et al., 2013) and New Polana (Bottke et al., 2015; Walsh et al., 2013). However, modeling when these families might produce a surge of impactors is challenging and requires detailed dynamical evolution work (e.g., Bottke et al., 2015).

The suggestion of a continual decrease in the impact flux in the last three billion years (e.g., Hartmann et al., 2007; Lagain et al., 2020) is consistent with our finding of the long-term lull indicated by D ≥ 100 km lunar craters. Our shorter-term lull at ~0.8–1.4 Ga has not been specifically found in any other data set that we know of, but some analyses, such as Mazrouei et al. (2019), indicate short-term lulls at other times, suggesting short-term decreases in impact flux are also plausible. We propose that the lulls occur because either asteroid families do not form at that time or near the strong resonances, as the background rate is likely too low for this size range to provide a constant flux at the levels expected for smaller impactors (e.g., Bottke et al., 2007; Fig. 1). In other words, consider the following. Objects entering resonances along the inner edge of the main belt (e.g., entering the nu6 secular resonance) have a nearly 1–2% probability of striking the Earth, but these probabilities decrease to 0.3%, 0.03%, and 0.01% for the 3:1, 5:2, and 2:1 mean motion resonances with Jupiter at 2.5, 2.8, and 3.3 au, respectively (Bottke et al., 2006). One can obtain impact probability values for...
system in the same relative sense with time as the smaller, sub-meter impactors. This difference in results for $D \geq 60$ km and $D \geq 50$ km has two implications: a) the variability in flux for $d \sim 5-6$ km (and possibly down to roughly several hundred meters; Mazrouei et al., 2019) is so strong that it overwhelms the lack of variability in the $d \sim 6-10$ km flux; and b) absolute model ages are not yet accurate enough to detect statistically significant spikes and lulls for all crater sizes examined. The former has some support in that smaller impactors should have a higher density than larger impactors (e.g., Bottke et al., 2007; Fig. 1). However, this would require a steeper than expected relative variation in the crater-size-frequency distribution with many more smaller impactors forming, which could have implications for how asteroids break up and the size distribution of the families is generated. Nevertheless, implication (b) is more likely in our opinion, given that uncertainties in absolute model ages are relatively large (Table 2). In addition, the histograms without uncertainties included for the other diameter ranges (Figs. 6b-e) appear to indicate weaker versions of the spike and lull seen for $D \geq 50$ in Fig. 6f, if those model ages are their medians.

5. Conclusions

In order to better understand the flux of km-sized asteroids into the Earth-Moon system over the last 3 Ga, we examined the crater retention model ages of $D = 50-200$ km lunar craters thought to have formed during the Copernican and Eratosthenian (Fig. 2, Tables 1, 2). This initial estimate of crater formation epoch was derived from crater morphologies and superpositions observed using Apollo imaging by the USGS (e.g., Wilhelms and McCauley, 1971) and Wilhelms (1987). Ages in this work are estimated by determining the density of small, superposed craters (diameters between 10s and 100s of meters up to a few kilometers) on the larger crater floors from LROC-WAC and NAC images and then using the Model Production Function (Marchi et al., 2009) (e.g., Figs. 3, 4). We assume that the flux of the small sub-kilometer impactors is exponential for $>3$ Ga and constant for $<3$ Ga as proposed by the standard lunar chronologies (e.g., Marchi et al., 2009; Neukum et al., 2001; Robbins, 2014). First, we have found that for some craters our model ages are older than the ages estimated from morphology and superposition (Table 2). For the craters that are still indicated to be $\leq 3$ Ga, we used a Kolmogorov-Smirnov test and Monte Carlo-type analyses to compute the statistical probability that the distribution of ages is not consistent with a constant flux as estimated by standard lunar chronologies for sub-km impactors (e.g., Marchi et al., 2009; Neukum et al., 2001; Robbins, 2014; e.g., Fig. 5). To understand if the flux changes with impactor diameter, we divided the distribution into diameter ranges starting with $D \geq 100$ km and decreasing that number by 10 until we got to the minimum of $D \geq 50$ km.

We find that the Earth-Moon impact flux may be variable for km-sized impactors. Our most statistically robust results indicate that the impact flux experiences a relative decrease, or “lull”, compared to the expected constant flux of sub-kilometer impactors (Fig. 6, Table 3). Furthermore, a less statistically robust result is that a 100–300 Myr relative increase in flux (“spike”) may occur $\sim 2$ Ga (Fig. 6, Table 3). Our results finding spikes and lulls is consistent with previous work using other datasets, such as radiometric ages of lunar glasses and rock abundance ages of lunar craters (e.g., Craddock and Howard, 2000; Culler et al., 2000; Grieve, 1984; Hartmann et al., 2007; Mazrouei et al., 2019; Schmitz et al., 2003). This potentially contradicts studies that have implied bias in these previous studies (e.g., Huang et al., 2018; Hui et al., 2009) and previous work that have indicated constant fluxes at all impactor diameters (e.g., Grier et al., 2001). However, with the uncertainty in crater retention model ages, we cannot come to any definitive conclusions on possible deviations in bombardment from a constant flux, particularly as it may change with diameter.

It has been proposed that a variation in flux could be caused by formation of asteroid families near strong orbital resonances with the

### Table 3
Plausible and possible spikes and lulls identified through the second Monte Carlo-type analysis.

<table>
<thead>
<tr>
<th>Crater set</th>
<th>Spike/Lull</th>
<th>Probability is spike/Lull</th>
<th>Age range (Ga), # of craters, # of permutations$^a$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D \geq 100$ km</td>
<td>Lull</td>
<td>$&gt;99%$</td>
<td>$0.0-3.0, 0$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$98%$</td>
<td>$0.0-2.6, 0$</td>
</tr>
<tr>
<td>$D \geq 90$ km</td>
<td>Lull</td>
<td>$95%$</td>
<td>$0.0-2.0, 0$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$96%$</td>
<td>$1.4-3.0, 0$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$96%$</td>
<td>$0.8-3.0, 1$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$95%$</td>
<td>$0.0-3.0, 2$</td>
</tr>
<tr>
<td>$D \geq 50$ km</td>
<td>Lull</td>
<td>$99%$</td>
<td>$0.8-1.4, 0, 6$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$97%$</td>
<td>$0.8-1.5, 1, 6$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$96%$</td>
<td>$0.8-2.0, 5, 6$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$95%$</td>
<td>$0.8-2.1, 6, 5$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$95%$</td>
<td>$0.3-2.0, 10, 4$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$95%$</td>
<td>$0.3-2.1, 11, 3$</td>
</tr>
<tr>
<td>Spike</td>
<td>$&gt;99%$</td>
<td>$2.1-2.2, 6, 6$</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>$99%$</td>
<td>$2.0-2.1, 7, 3$</td>
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<td>$98%$</td>
<td>$2.0-2.6, 11, 3$</td>
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<td></td>
<td>$96%$</td>
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<td>$96%$</td>
<td>$2.0-2.4, 8, 3$</td>
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<td></td>
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<td>$95%$</td>
<td>$2.0-2.5, 9, 3$</td>
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<td>$95%$</td>
<td>$1.6-2.2, 10, 3$</td>
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<td>$1.5-2.2, 11, 5$</td>
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<td>$95%$</td>
<td>$1.4-2.2, 12, 4$</td>
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</tr>
<tr>
<td></td>
<td></td>
<td>$95%$</td>
<td>$1.4-2.6, 16, 3$</td>
</tr>
</tbody>
</table>

$^a$ The number of permutations each spike or lull is observed in is only listed for $D \geq 50$ km crater group. Spikes or lulls with $< 3$ permutation occurrences are listed in Supplemental Table S2.
gas giants in the Main Asteroid Belt (e.g., Bottke et al., 2007; Vokrouhlický et al., 2017; Fig. 1). Our results could support this idea as the possible spike is occurring at a time when some large asteroid families(y) near resonances are suggested to occur (e.g., Bottke et al., 2006; Nesvorný et al., 2015). We further suggest that the possible lulls then occur because either asteroid families are not forming at that time or do not form near resonances that would move asteroids effectively into the Earth-Moon system, since the average background rate may not be high enough to regularly produce impacts (e.g., Bottke et al., 2007; Fig. 1).

Declaration of competing interest

None.

Acknowledgments

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Appendix A. Supplementary data

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eferences


