

# Simulations of Volcanic Plumes and Aurora on Io by the ASE/Astro “Io Group”

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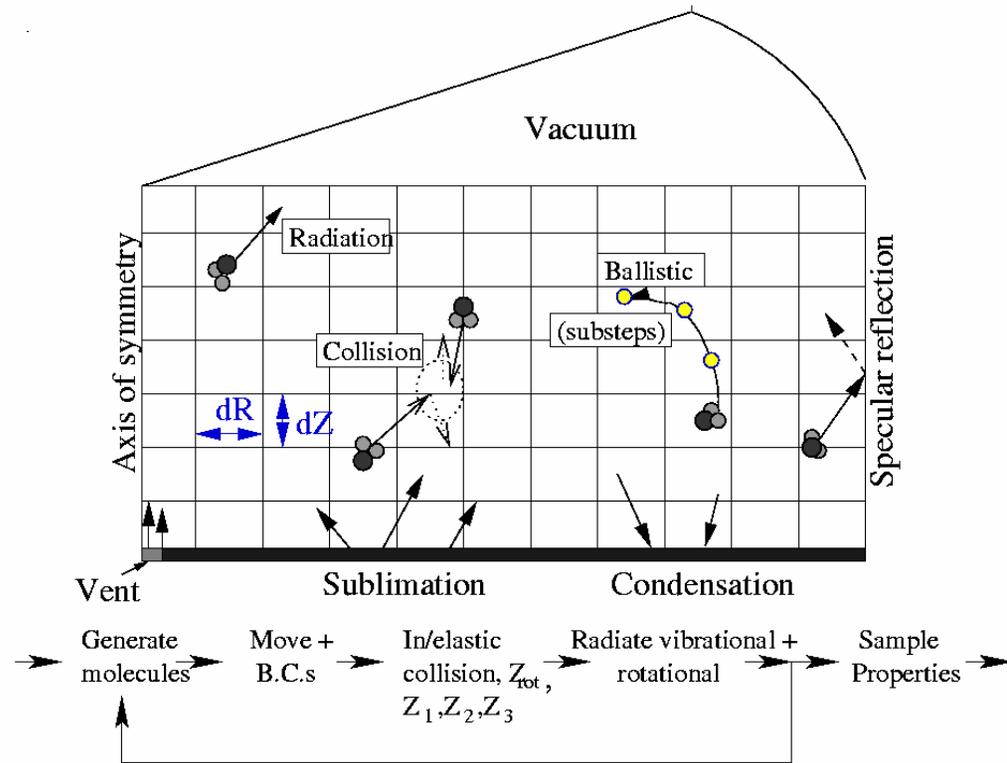
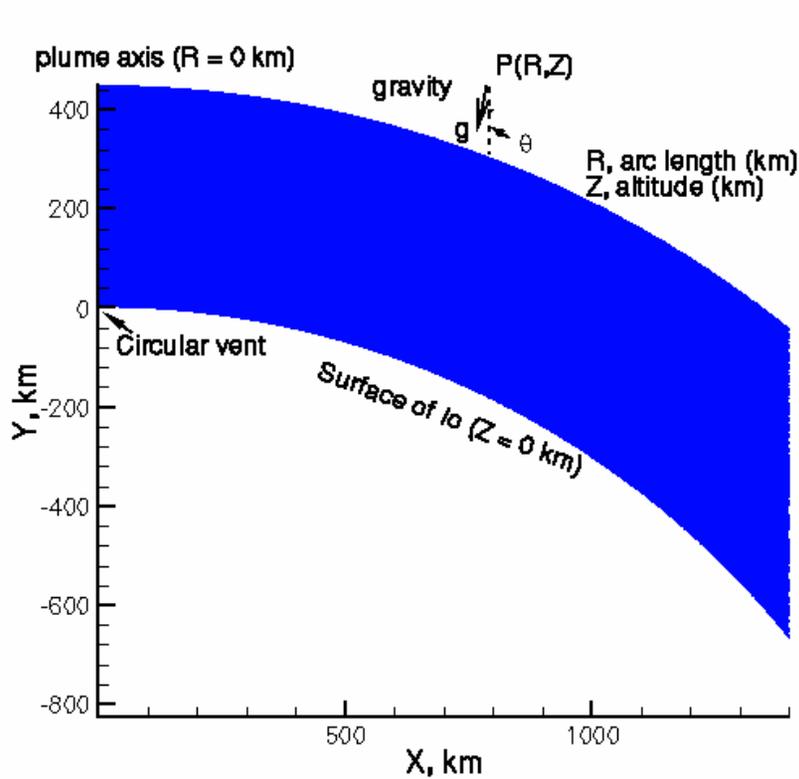
# Two talks for the price of one

- Background on Io's volcanic plumes
- Numerical methods and basic features associated with simulated plumes
  - Flow Conditions (example results)
  - Innovations DSMC methods (VT energy transfer, etc.)
  - Gas/particle flow modeling
- Matching observations with the simulations
  - Parametric study on vent conditions
  - Reproducing Voyager plume images by gas and dust flow
  - Plume deposition profiles

And then.....

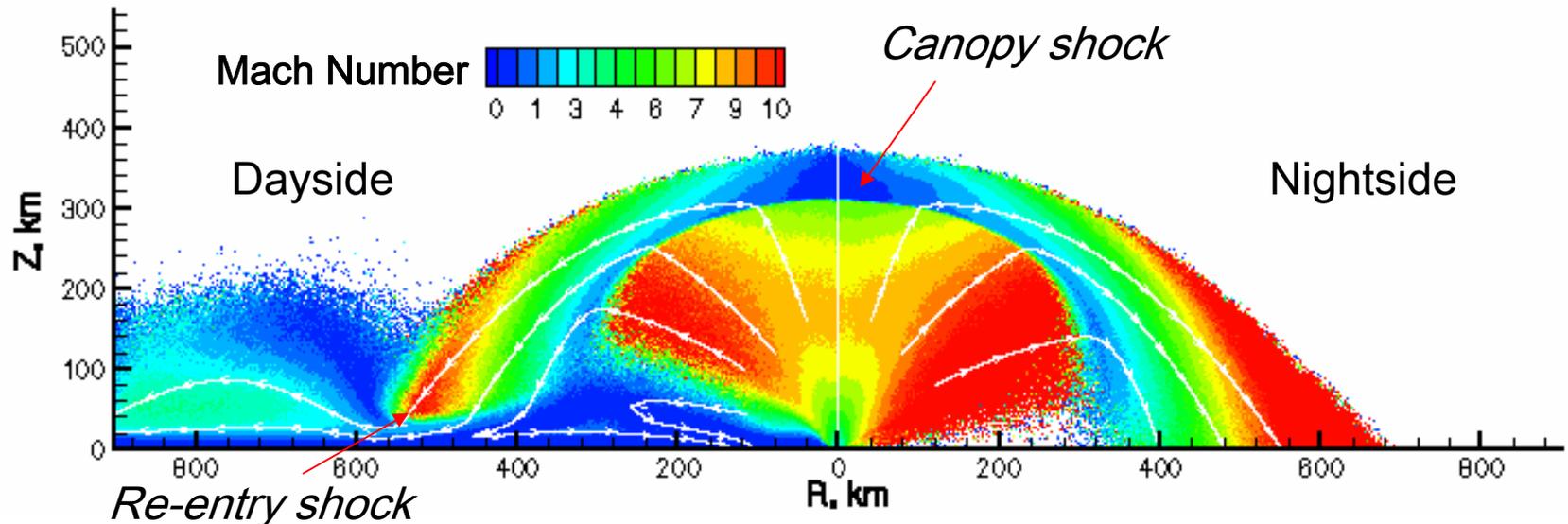
- Background on Io's aurora
- Numerical simulations of electron motion and Io's full atmosphere
- Why does the wake glow?

# Schematic of Flow Conditions



- DSMC (direct simulation Monte Carlo) Method;
- Suitable for rarefied gas dynamic applications on Io;
- Axisymmetric flow; spherical geometry
- Vibrational and rotational energy exchange;
- Infrared and microwave radiation;
- Two phase gas/particle flow

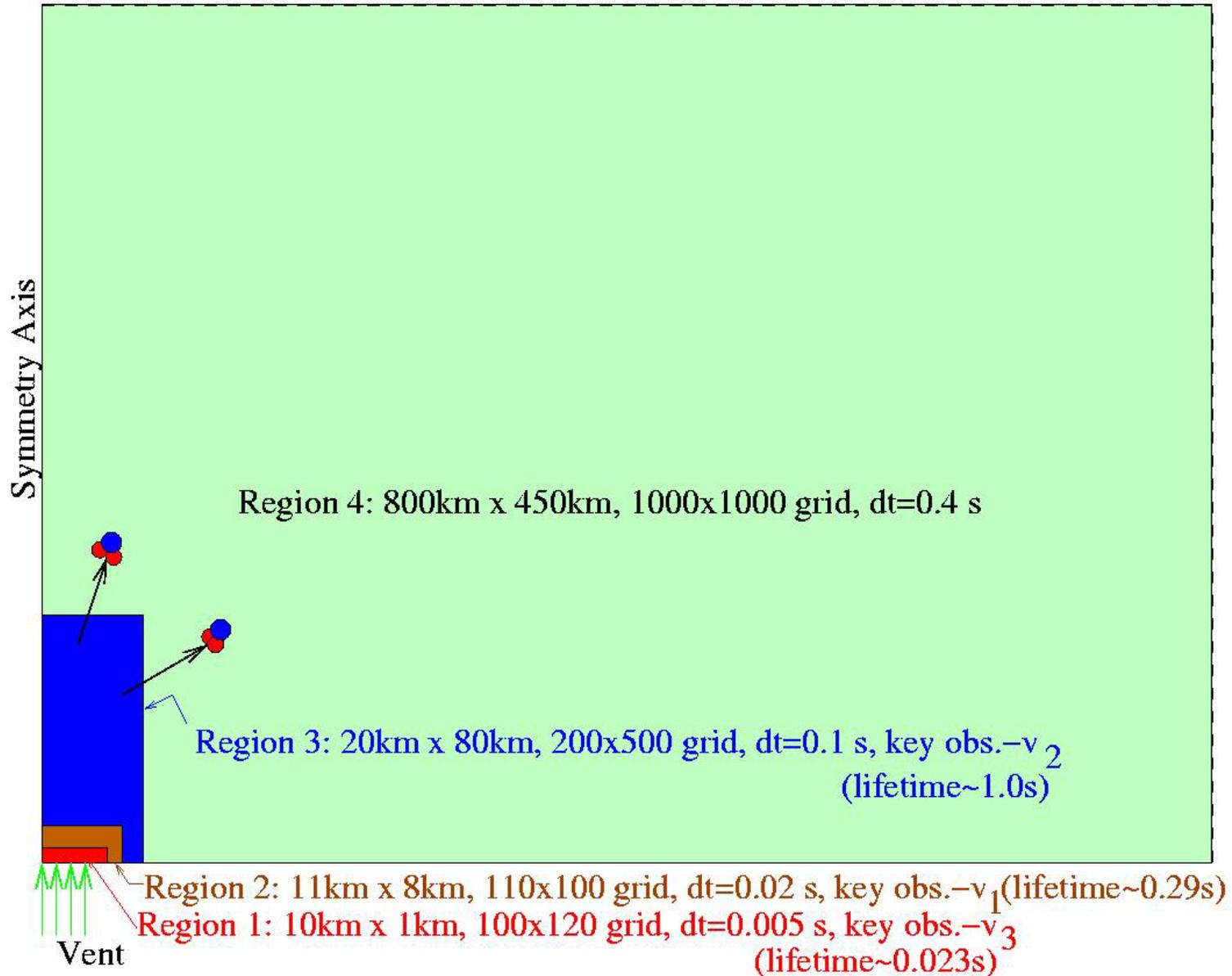
# Basic Flow Features in Simulated Plumes



Comparison of Mach number contours of dayside (left,  $T_s = 115$  K) and nightside (right,  $T_s = 90$  K) Pele type plume.

- $\text{SO}_2$  gas erupts from the vent (located at  $R = 0$  km) at around Mach 3, expands, accelerates, until gravity slows it down.
- A canopy shaped shock is formed at an altitude of about 300 km
- A re-entry shock is formed for plume on dayside

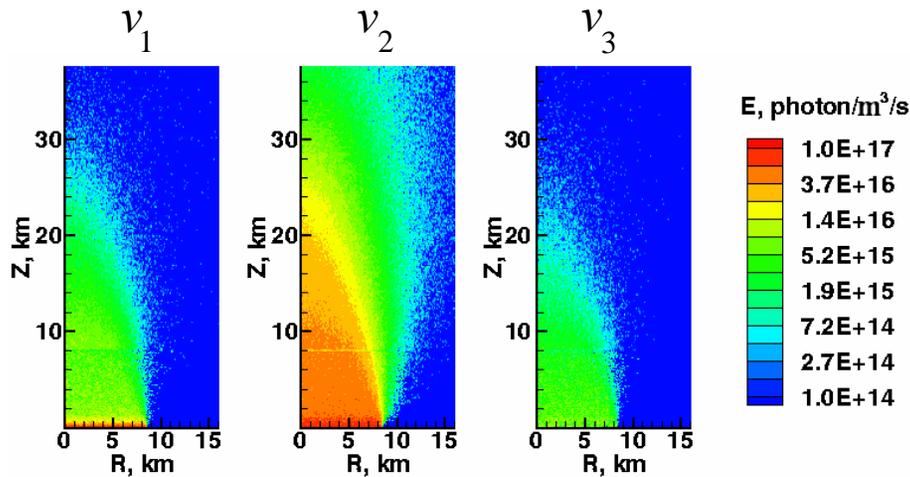
# Decomposition of the Computational Domain



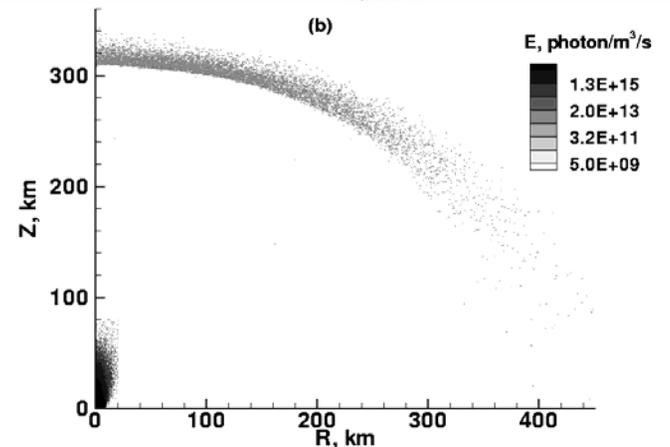
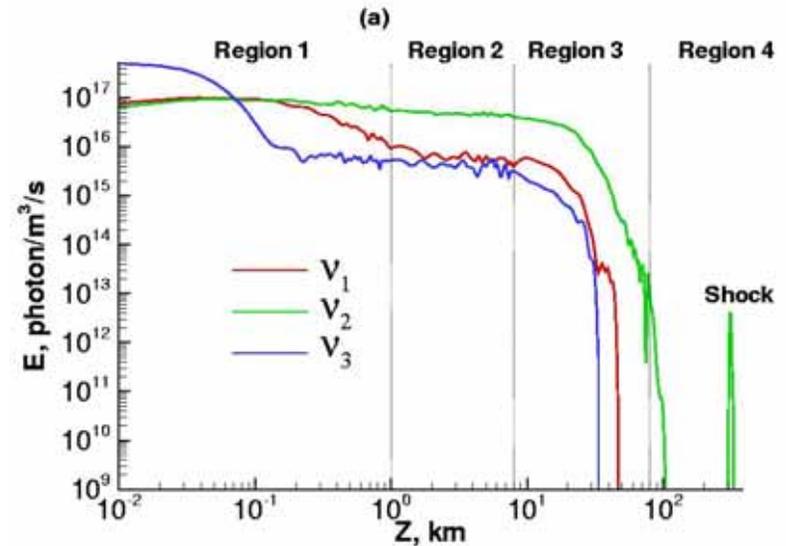
# DSMC Emission Results for Pele Type Plume

- $\nu_1$  and  $\nu_3$  band emission rates drops one order of magnitude within 2 km. The rapid emission signatures are captured by calculation in region 1 and 2 with very fine spatial and temporal resolutions.

- Emission from  $\nu_2$  band re-appears at the shock.

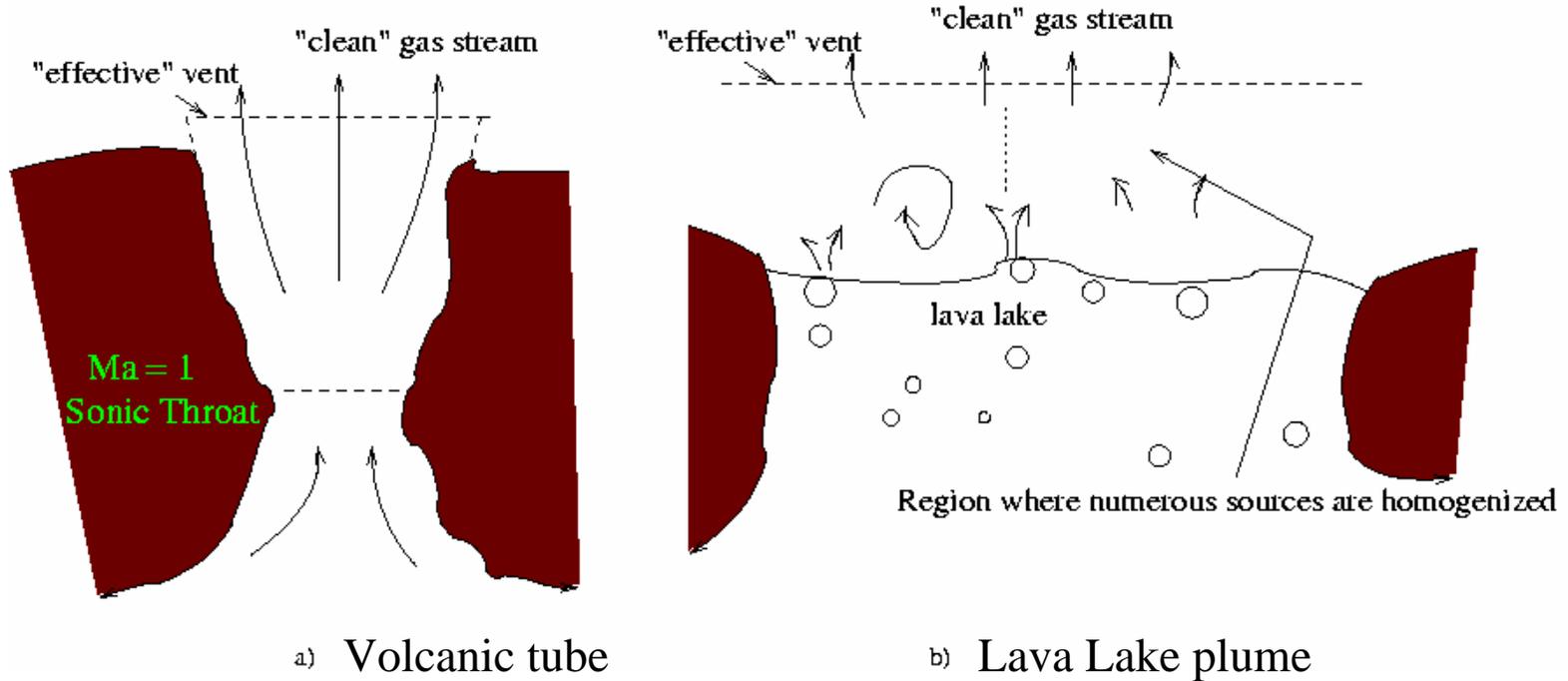


DSMC calculated photon emission rate contours for  $\nu_1$ ,  $\nu_2$  and  $\nu_3$  vibrational bands near the plume core.



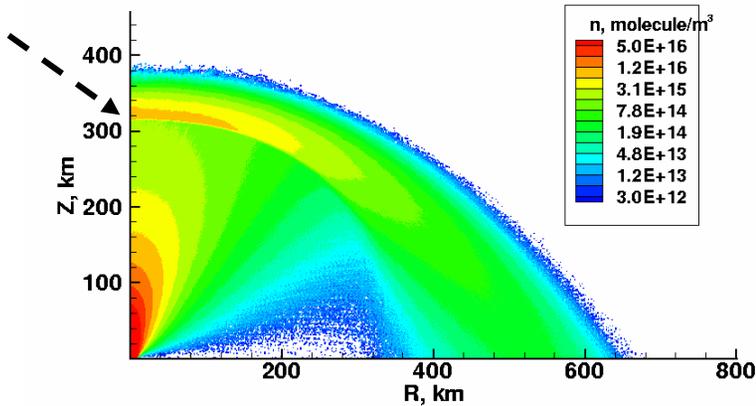
Profiles of emission rate along symmetry axis and contours of emission rate for  $\nu_2$  band.

# What are conditions at the “Effective” Vent

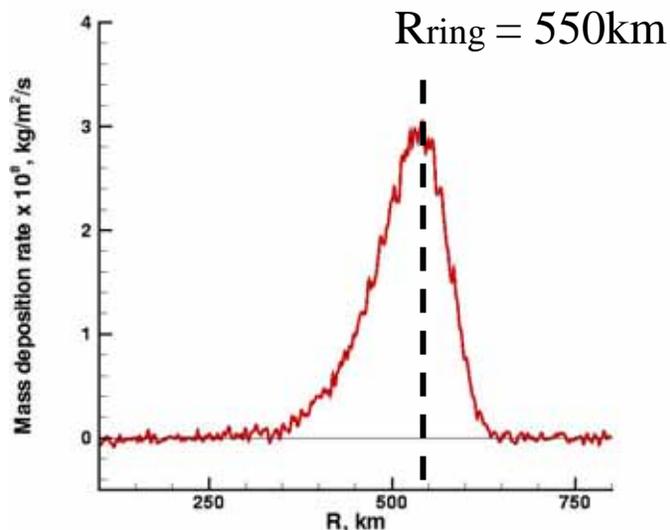


# Parametric Study of Vent Conditions ( $T_{\text{vent}}$ , $V_{\text{vent}}$ )

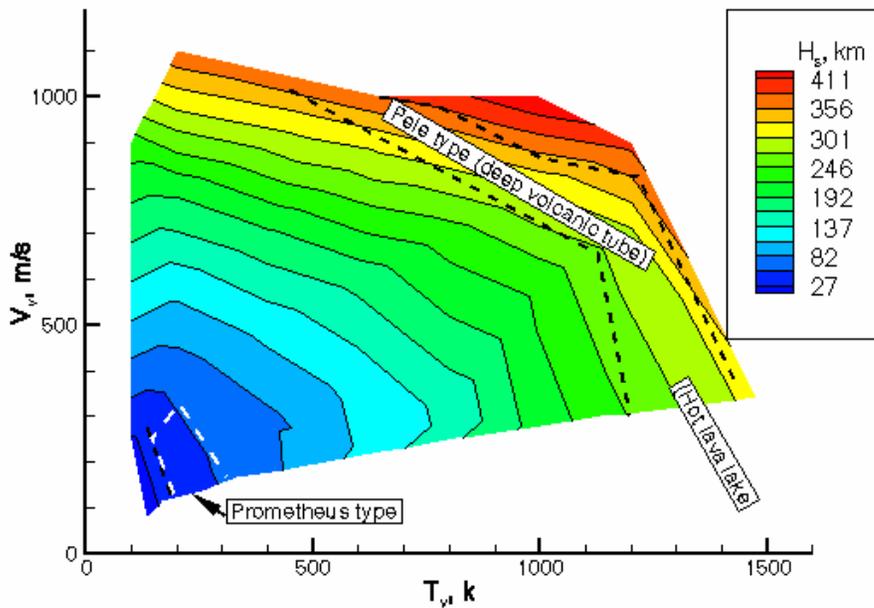
$H_{\text{shock}} = 320 \text{ km}$



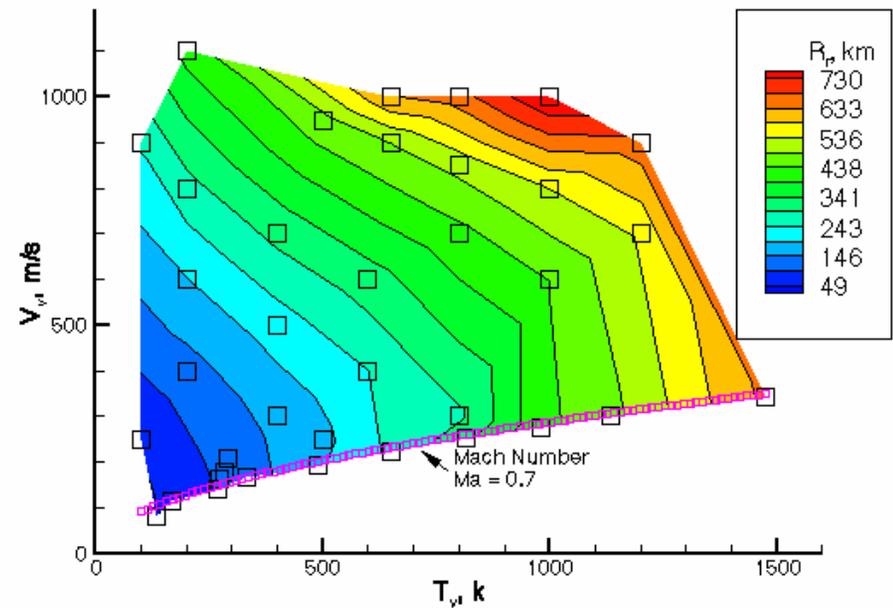
- Shock height and deposition depend on vent conditions.
- Goal: using parametric study results to constrain vent conditions based on observed shock height and peak deposition radius.
- Assumptions include fixed number density at the vent; optically thin gas;  $\sim 8 \text{ km}$  vent radius; night side plume.



# Parametric Study of Vent Conditions ( $T_{vent}$ , $V_{vent}$ )



Constant shock height ( $H_s$ )



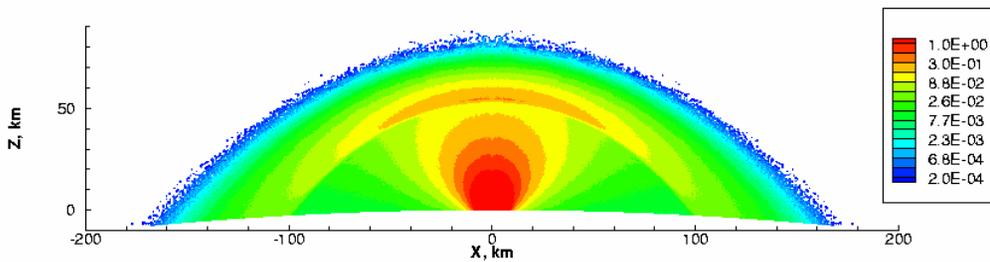
Constant peak deposition ring radius ( $R_r$ ).

- Similar figures for other properties, such as the total mass, total emission power from each band, etc.

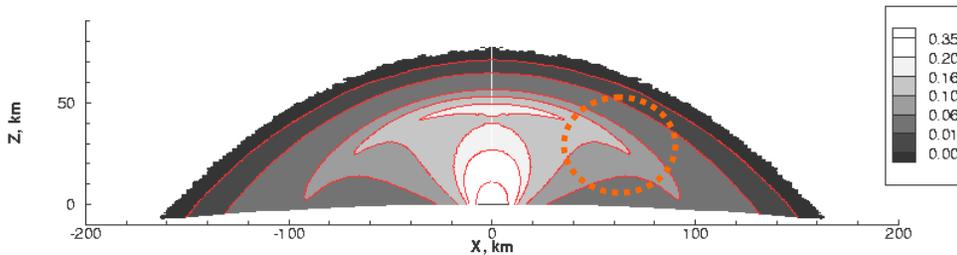
# Matching Voyager Image of Prometheus



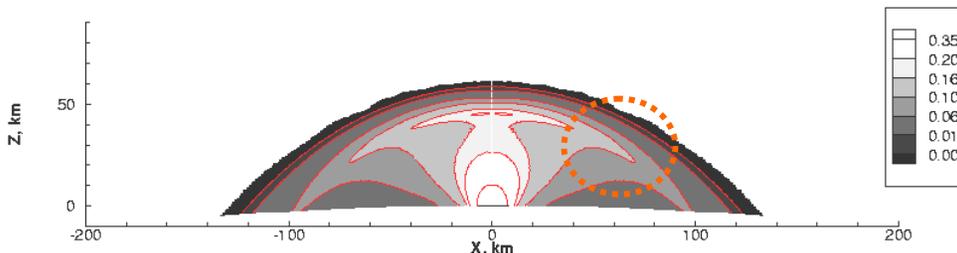
a) Voyager image



b) Gas number density



c) Gas column density (tangential)



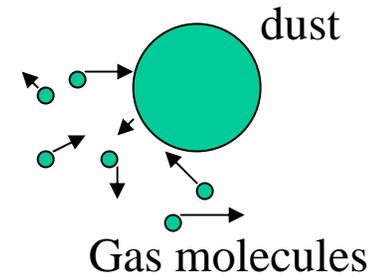
d) 1 nm particle column density (tangential)

- **Encouraging semi-quantitative similarities of the integrated gas column density to the Voyager image (Strom & Schneider, 1981) of Prometheus.**
- **The Voyager image likely shows the solar reflection of the fine particulates in the plume (<10 nm, Collins 1981).**
- **The column density of 1 nm refractory particle plumes indeed shows convincing similarities to the Voyager image as does the gas.**

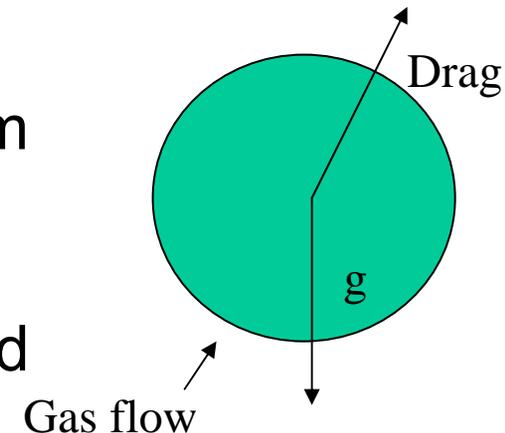
# Gas/particle Flow Modeling

Two “Overlay” Methods (assuming dilute particle flow) —  
Particles are assumed to be spherical, refractory and have a density of liquid SO<sub>2</sub>.

- i) Gas/particle collision model (costly for 1 micron and larger particles).
- ii) Drag model (assuming free-molecular flow — particle diameter based  $Kn \gg 1$ ,  $C_d = f(s)$  (Bird, 1994).)

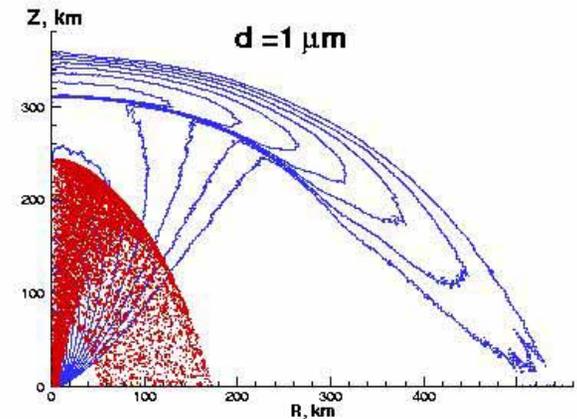
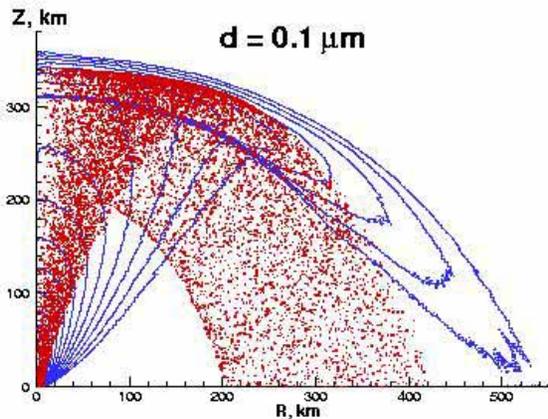
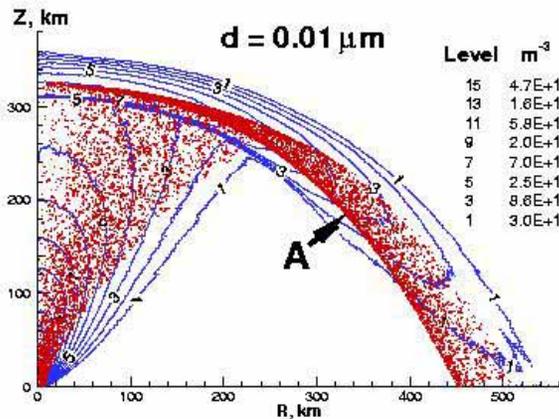


1. Obtain smooth steady gas flowfield
2. Release particles at zero velocity from the vent and calculate the drag on the particle.
3. Calculate acceleration of particles and move them

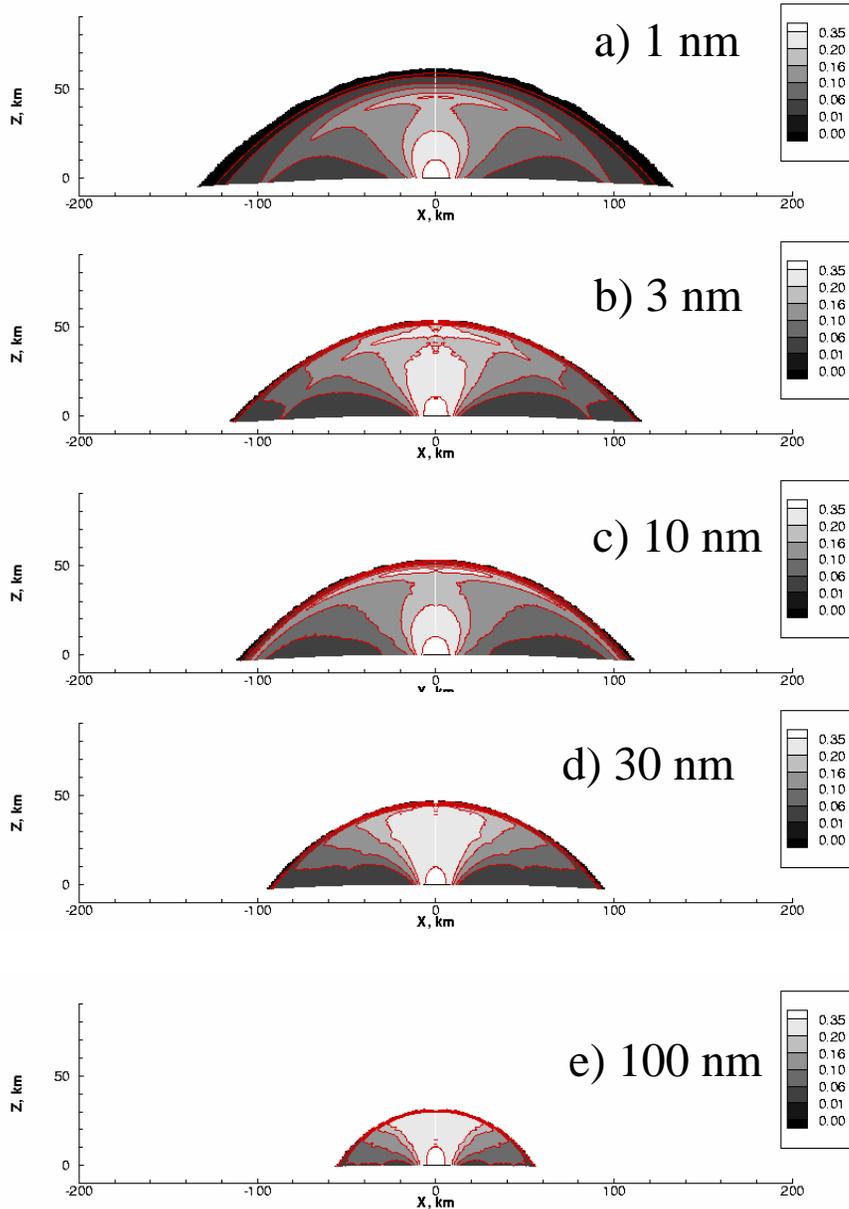


# Gas/particle Flow

- Concentration of particles near the shock is seen for particle with size of  $0.01 \mu\text{m}$  up to  $0.1 \mu\text{m}$  (agree with size range analyzed by Collins '81)
- A sorting of particles by size inside the plume and on the surface
  - finer particles falling further away from the vent
  - large particles stay close to the axis and land close to the vent



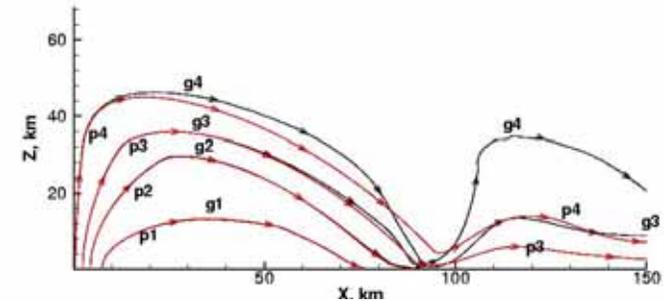
# Parametric Study of Particle Size



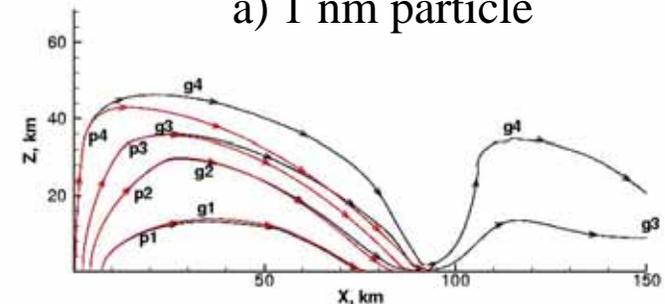
- Small particles ( $\sim 1$  nm) track gas flow well, reproduce plume image in the outer portion of the plume.
- Decoupling between gas and particle motion starts early for large particles.
- Upper limit of particle size in the outer portion of the plume is 10 nm, consistent with Collins 1981.

# Particle Size Dependence of the Response Behavior

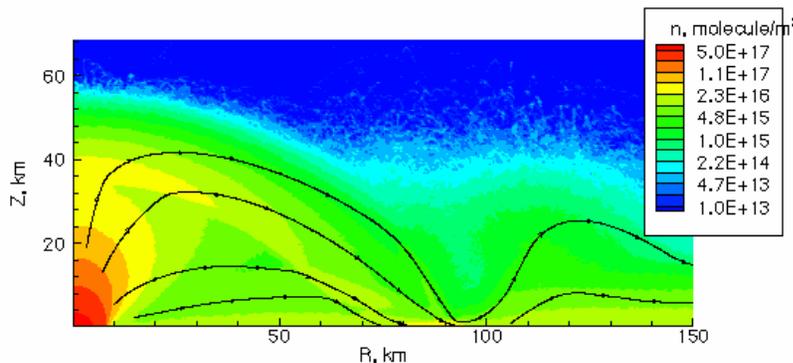
- 1 nm particle tracks the gas flow well.
- Larger particles are less responsive to the accelerating gas flow.
- The turning flow near the re-entry shock acts like a cyclone separator: the larger particles are sorted from the small ones.



a) 1 nm particle

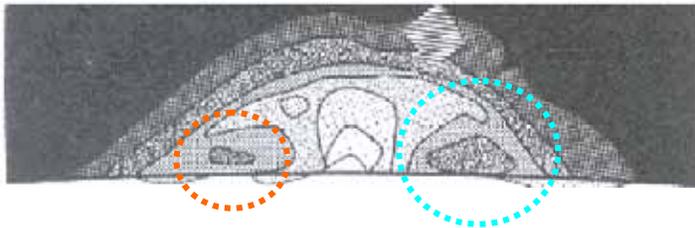
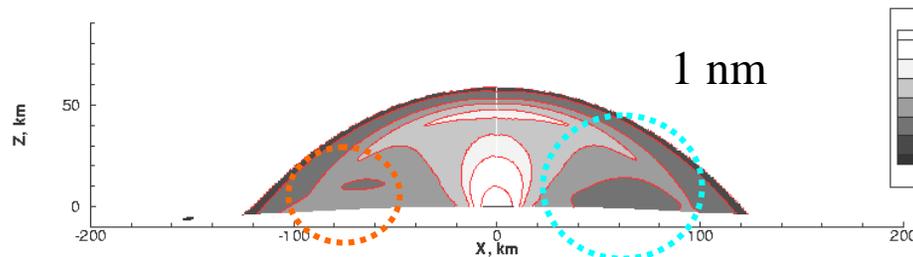
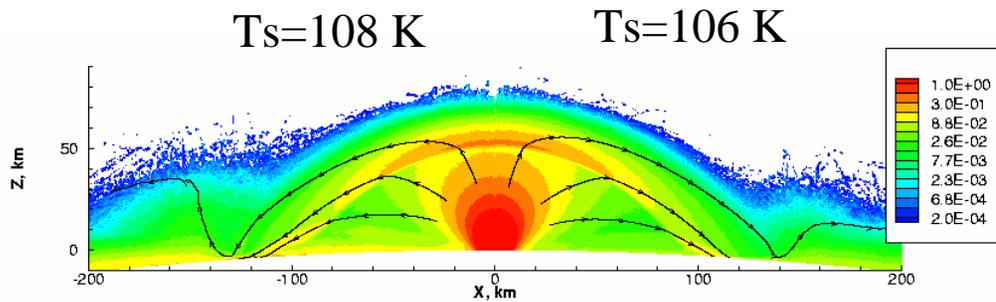


b) 3 nm particle

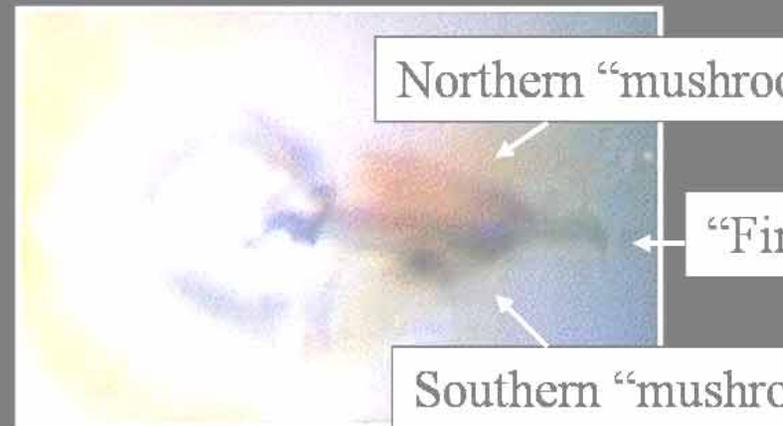
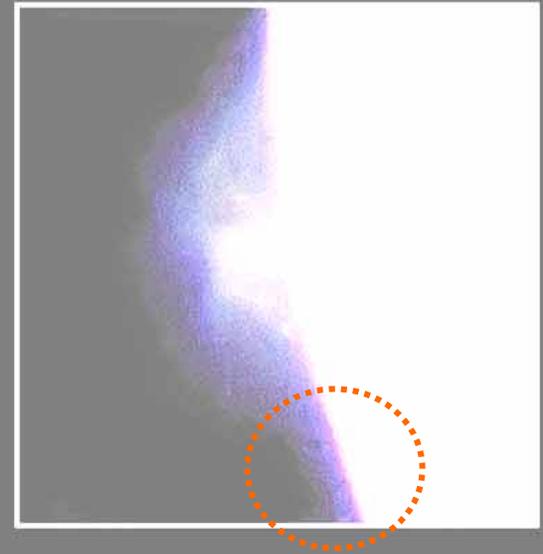
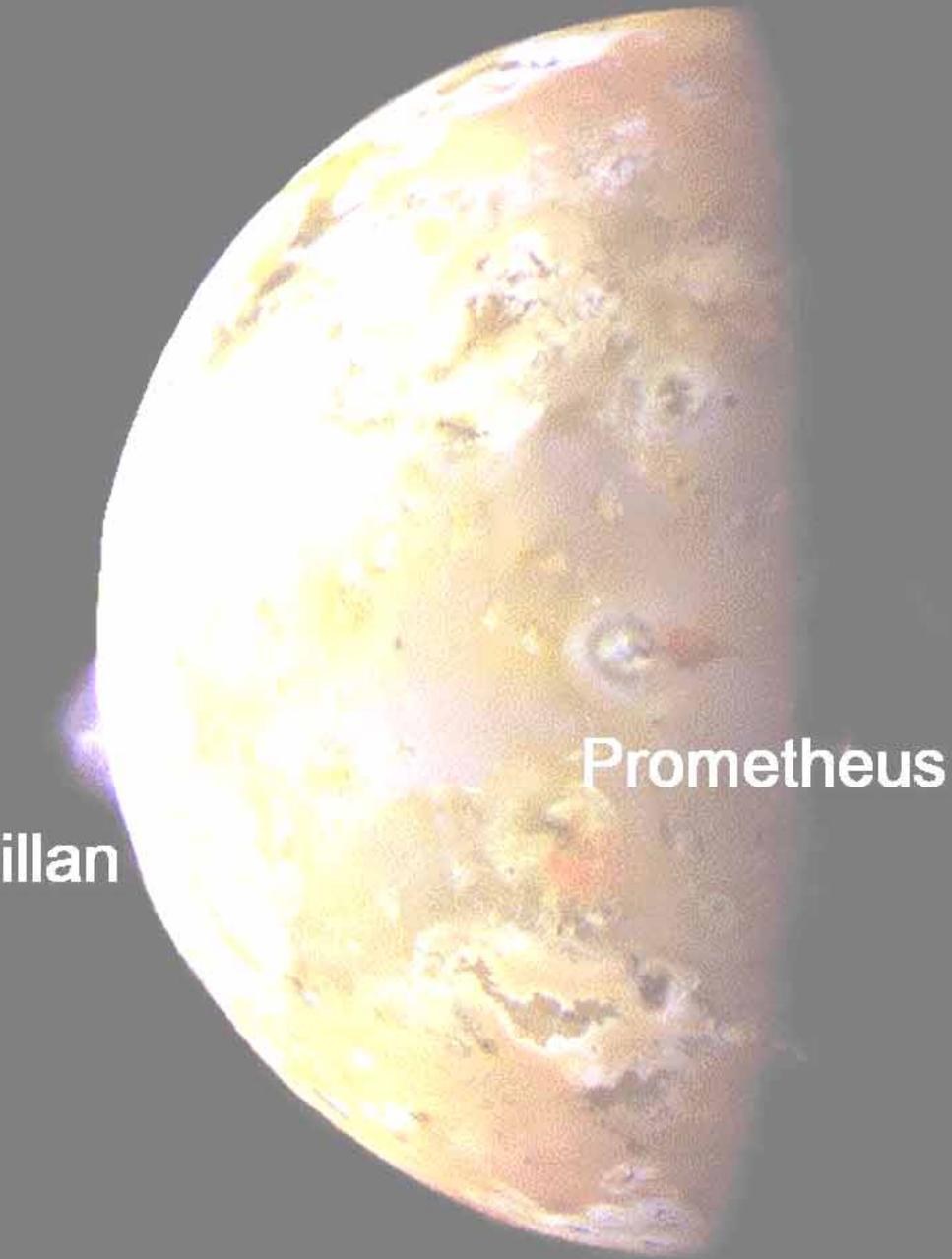


Comparisons of gas streamlines (black) and trajectories of entrained particles (red). The surface temperature is 110 K and the gas number density contours are shown on the left.

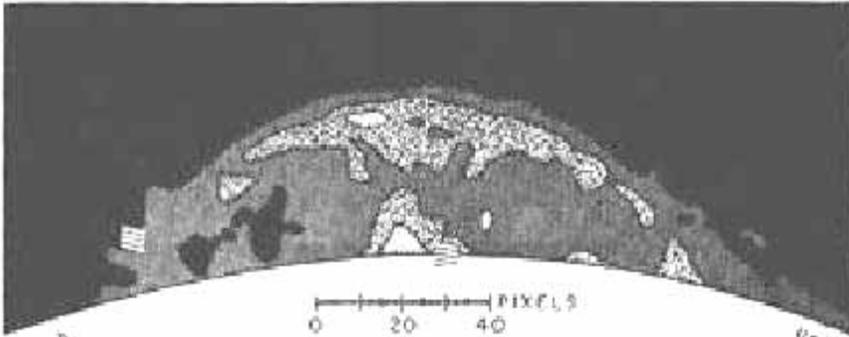
# Matching Voyager Image of Prometheus



- A relatively high brightness near the surface (within  $\sim 5\text{ km}$  above the surface on the left side of the plume) is also seen in the Voyager image of Prometheus indicating a high particle column density there.
- This feature can also be reproduced by a plume of nano-size particle at a slightly higher surface temperature.

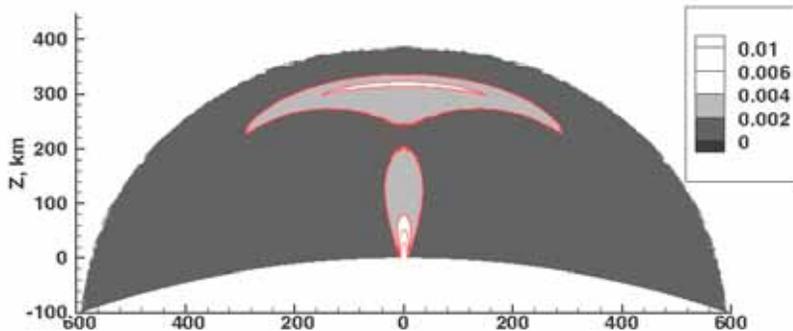


# Matching Voyager Image of Pele

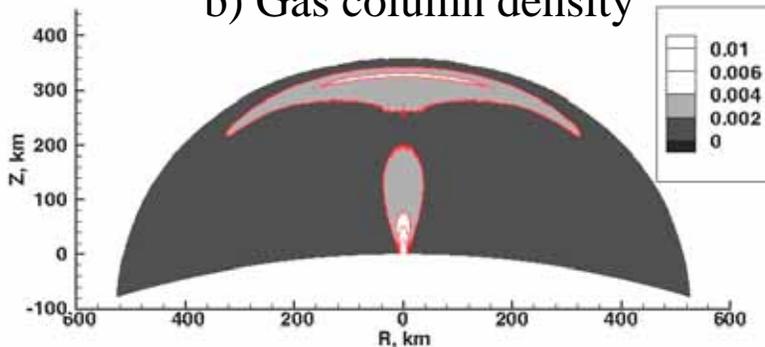


a) Voyager image of Pele

- Such qualitative similarities were also found for Pele.



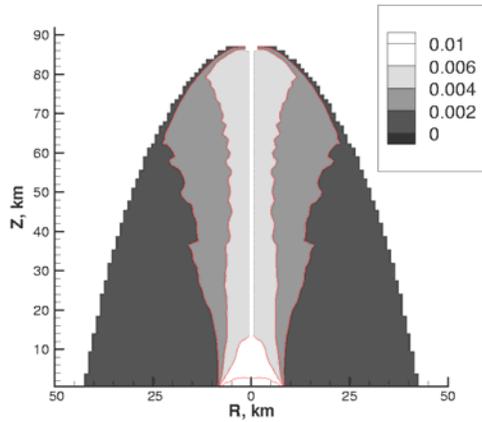
b) Gas column density



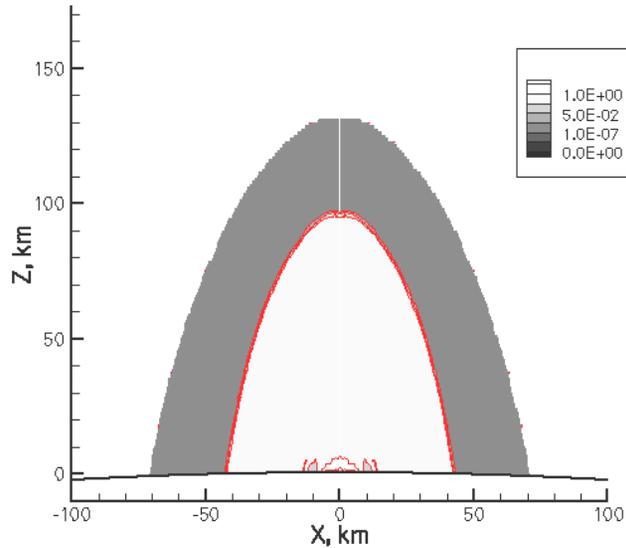
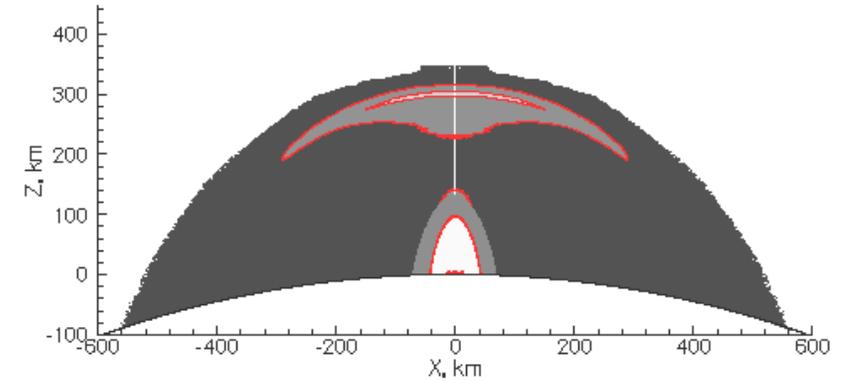
c) 1 nm particle column density

- The “cone” shape contours in the vent vicinity in the Voyager image cannot be reproduced by 1 nm particle plume.

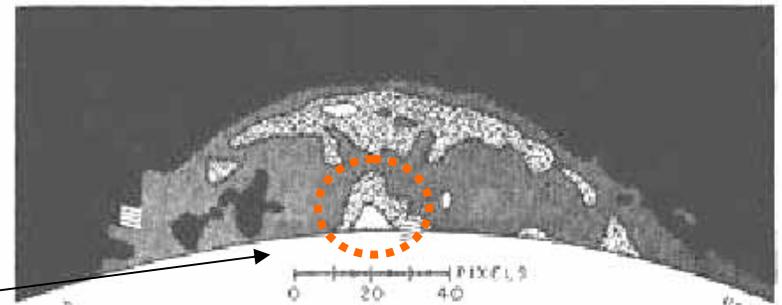
# Matching Voyager Image of Pele



a) 10 micron

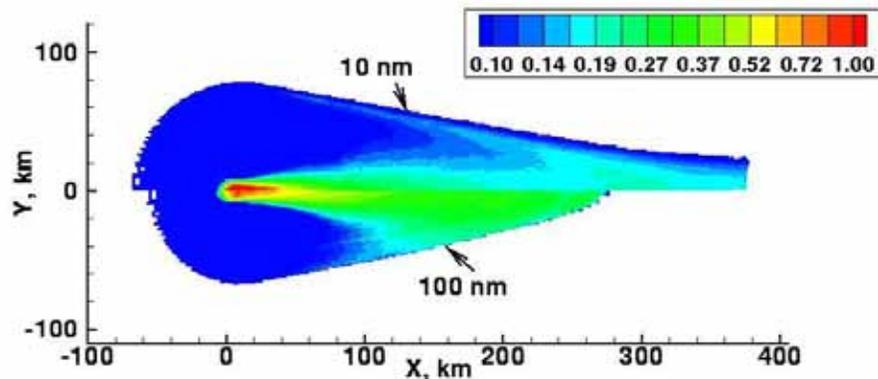
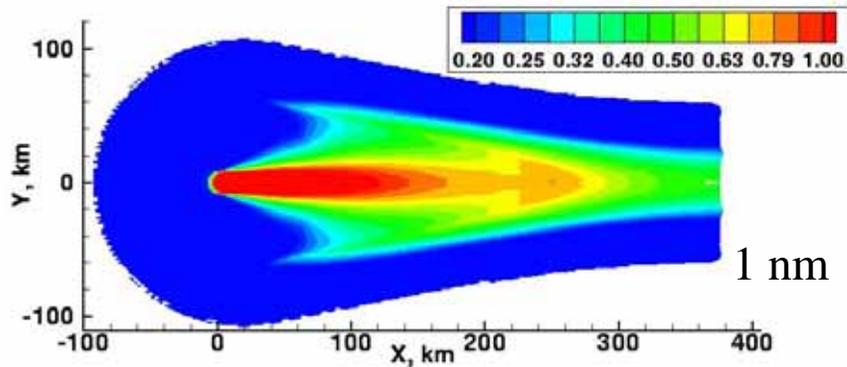
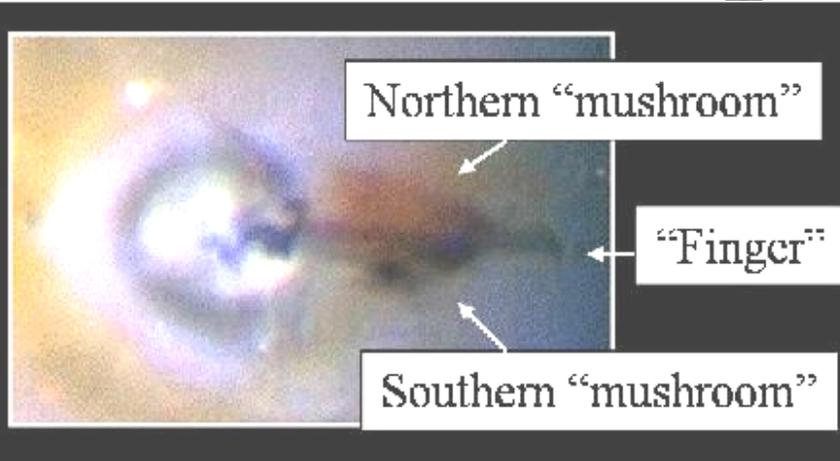


b) Log normal size distribution (5-10 micron) with  $r^6$  size-dependent scatter efficiency.



c) Better match to Voyager image

# Matching Plume Shadow



- A remarkable reddish shadow cast by Prometheus is seen in the Galileo image.
- The solar zenith angle at the Prometheus vent is  $\sim 78^\circ$ . The column densities projected from the sun onto Io's surface at this angle were calculated.
- The "finger" shape is found to be best reproduced by a plume of  $\sim 10$ - $100$  nm particles. The "mushroom" shape may be reproduced by 1 nm particles.

# Reproducing the Multiple Ring Deposition Structure around Prometheus

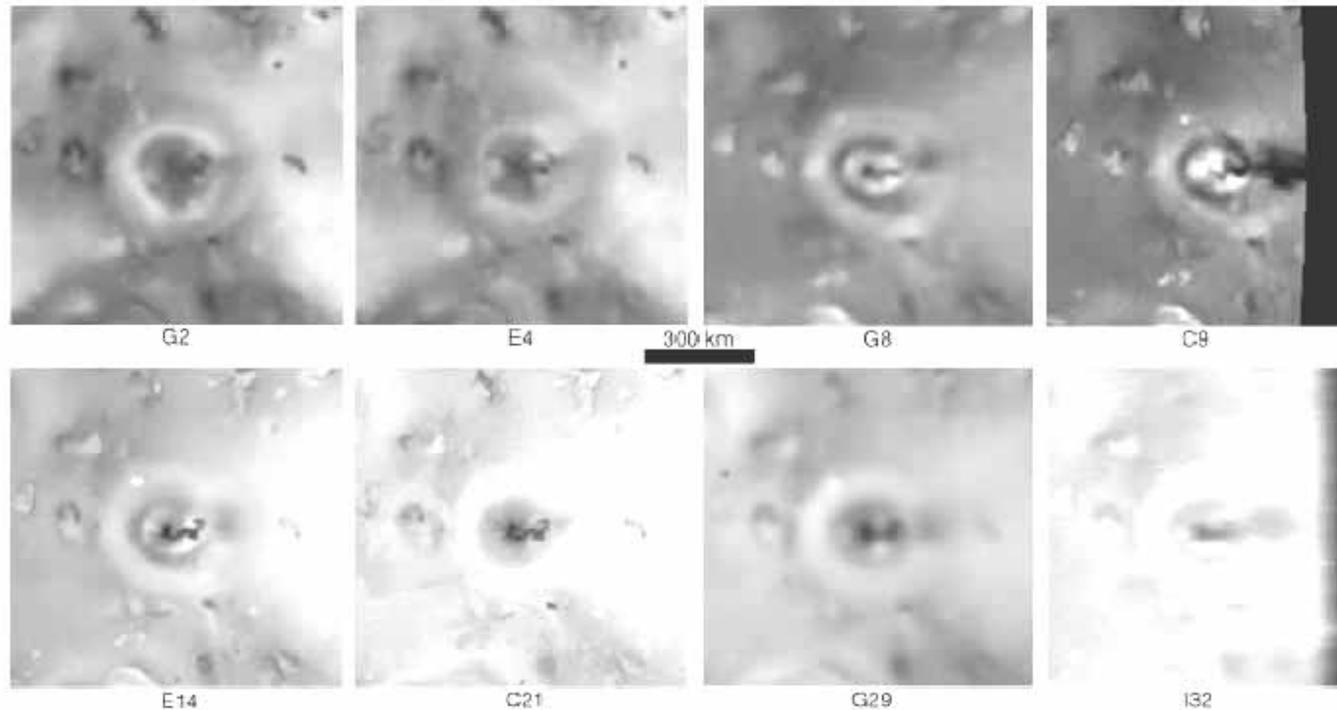
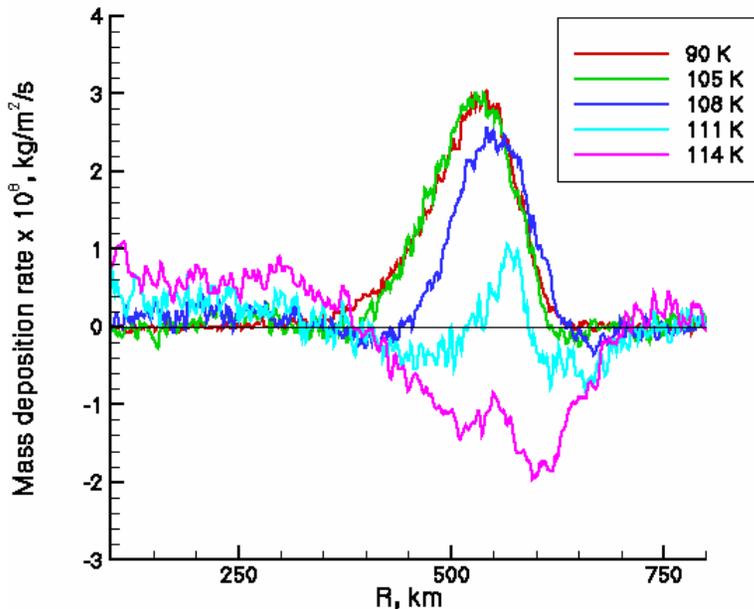
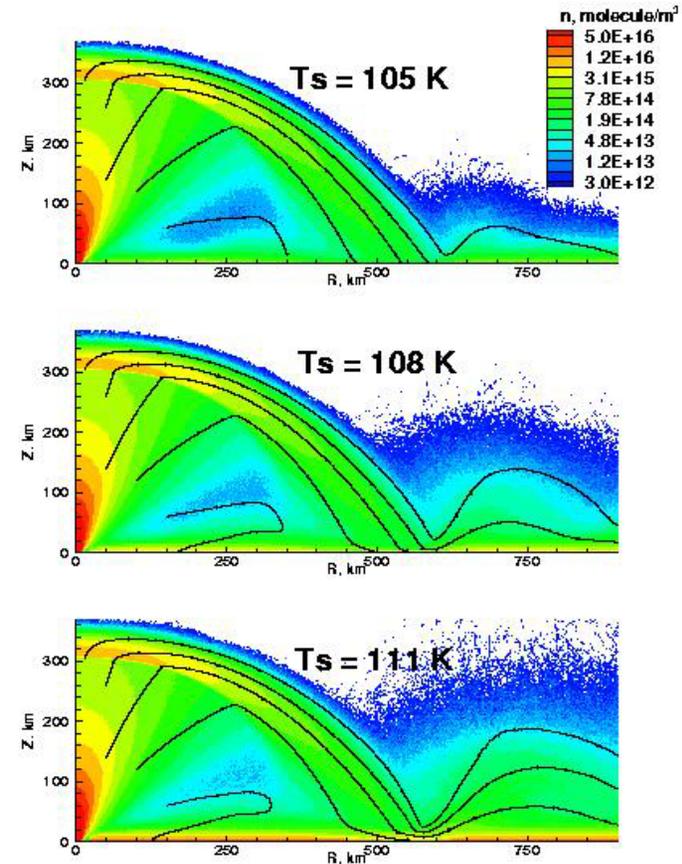


Figure 10. Surface changes at Prometheus. Violet filter images.

Geissler *et al*, 2003

# Parametric Study on Surface Temperature

- At low surface temperature, the falling gas simply pours onto the ground and condenses unimpeded.
- As the surface temperature rises to  $\sim 111$  K, a nearly horizontal re-entry shock and well defined bounce region are formed.
- Deposition ring forms at  $R = \sim 500$  km.
- Depletion effects appear at high surface temperature.



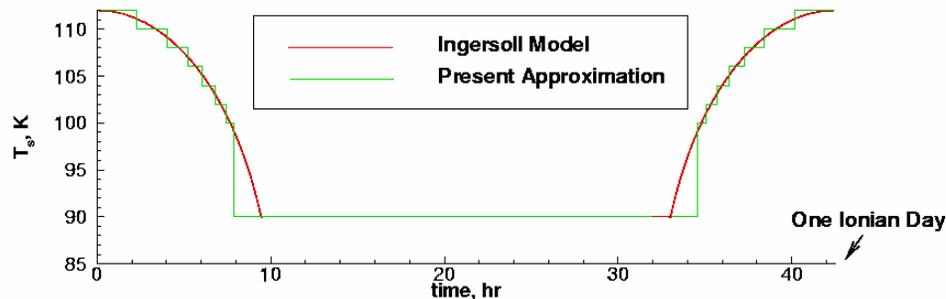
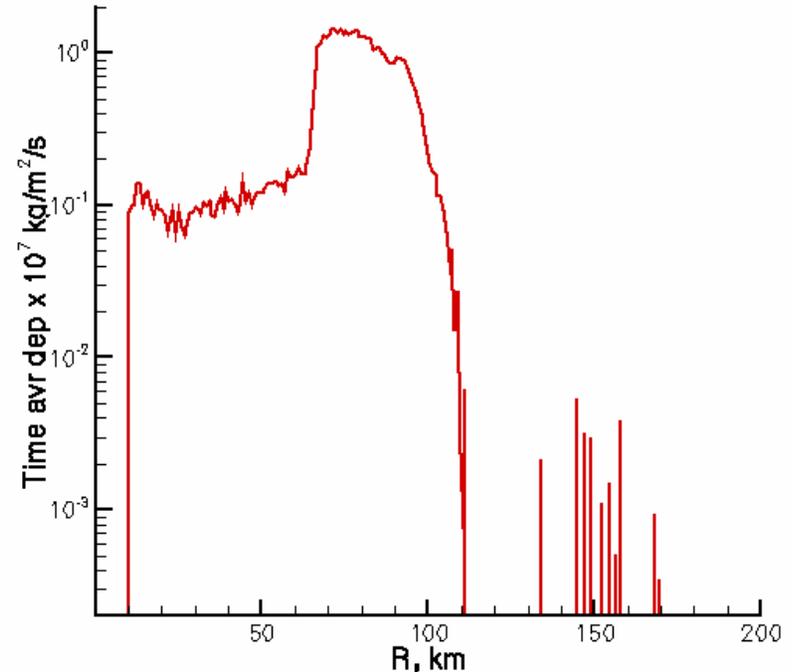
Number density contours with different surface temperature (right) and profiles of deposition rate (left).

# Gas Deposition Pattern around Prome

- Gas deposition pattern varies as surface temperature changes.
- No multiple rings structure is seen in the time averaged deposition profile.
- May imply that the source strength is unsteady.
- However, “bounce” in the flow and/or dust deposition may be other possible causes of the multiple ring structure.

$$T_s = (T_{\text{subsolar}} - 50) \cos^{1/4} \theta + 50$$

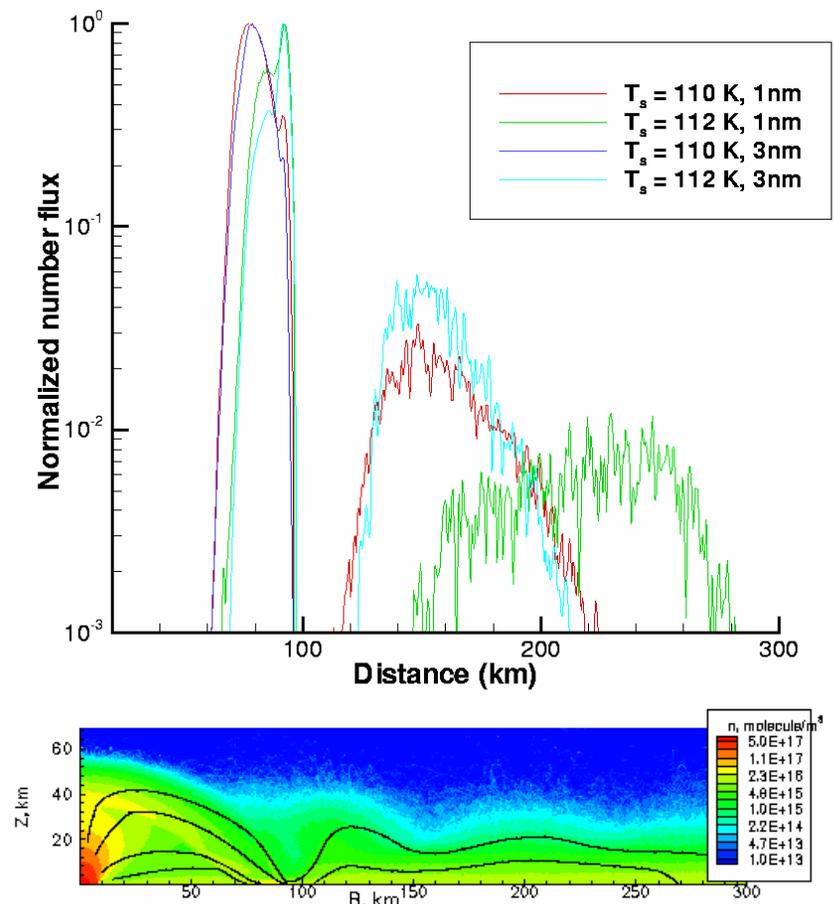
Ingersoll, *et al*, 1985



b) Surface temperature as a function of time

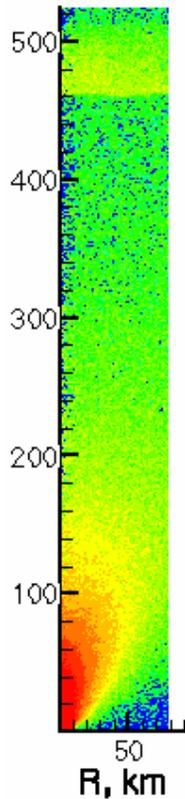
# Particle Deposition Pattern around Prometheus

- The deposition of nano-particles in plumes with relatively high surface temperatures are examined.
- Due to the “bouncing” with the gas flow, outer rings are indeed seen in the nano-particle deposition profiles.

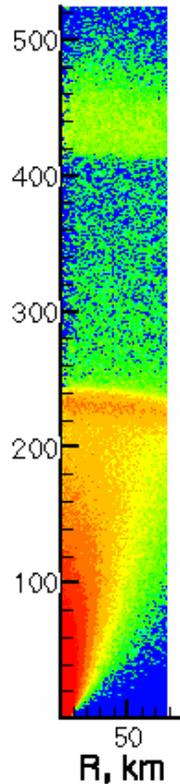


# The Effects of Unsteadiness of Volcanic Sources

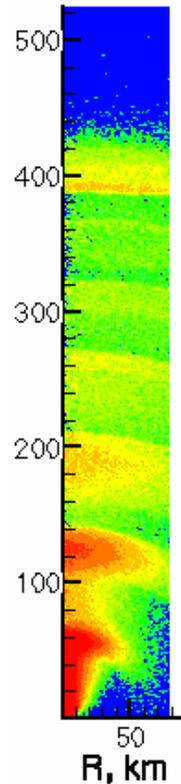
a) 30 min.



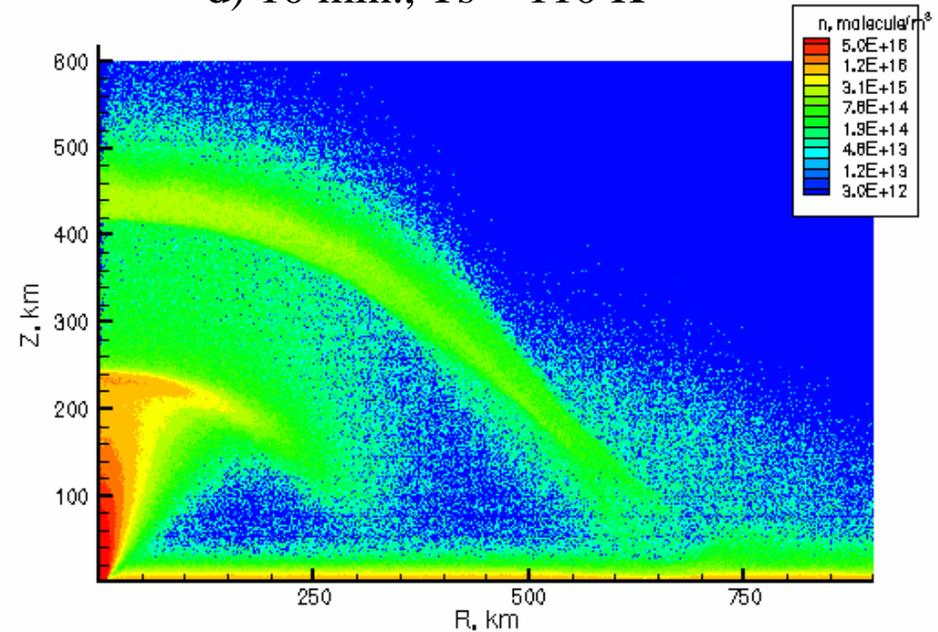
b) 10 min.



c) 1 min.



d) 10 min.,  $T_s = 110$  K

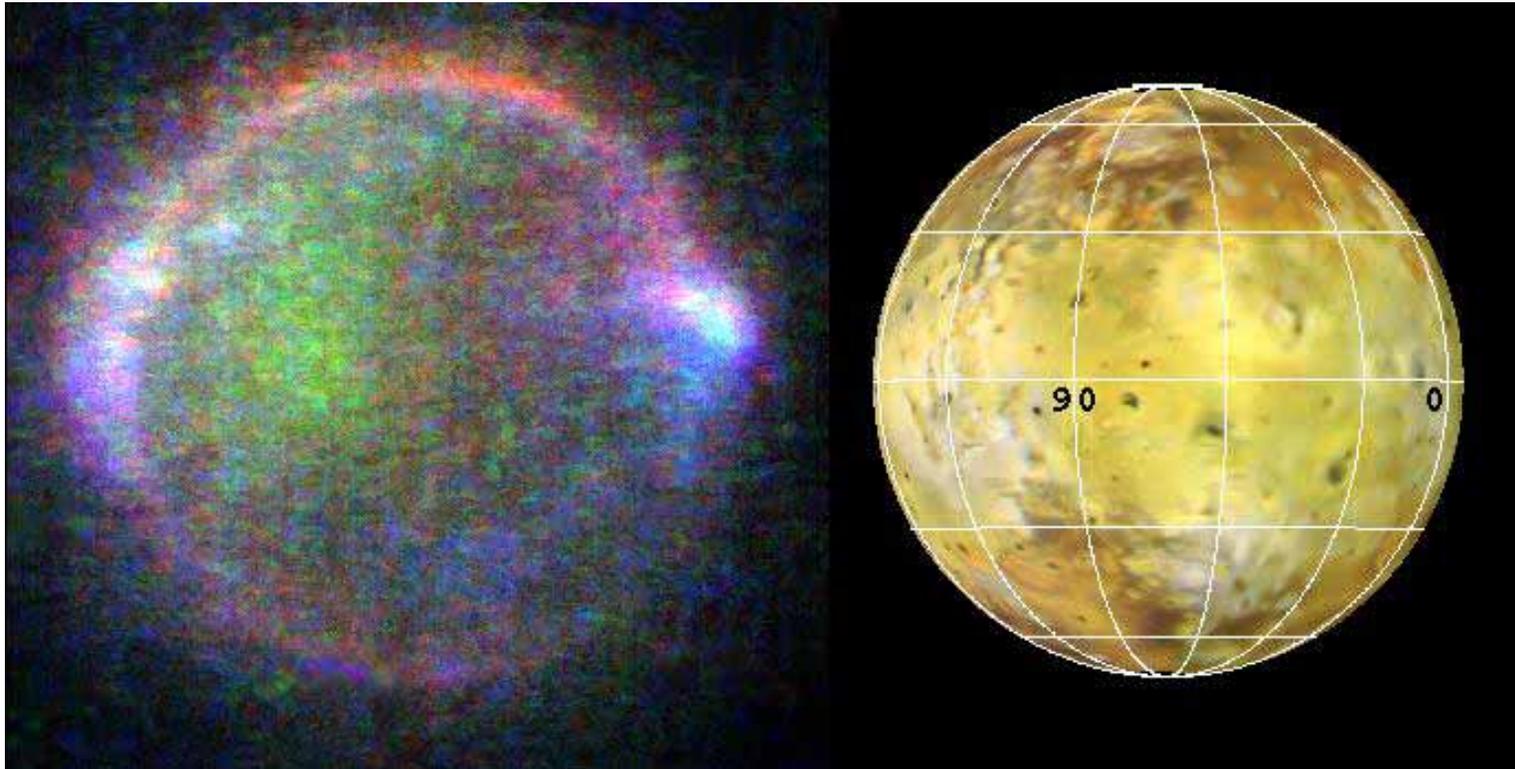


- $V_v$  is pulsed sinusoidally. Other parameters kept constant.
- Stronger moving shocks for long period pulsing.
- Stationary shock for very short period pulsing.

# Plume Conclusions

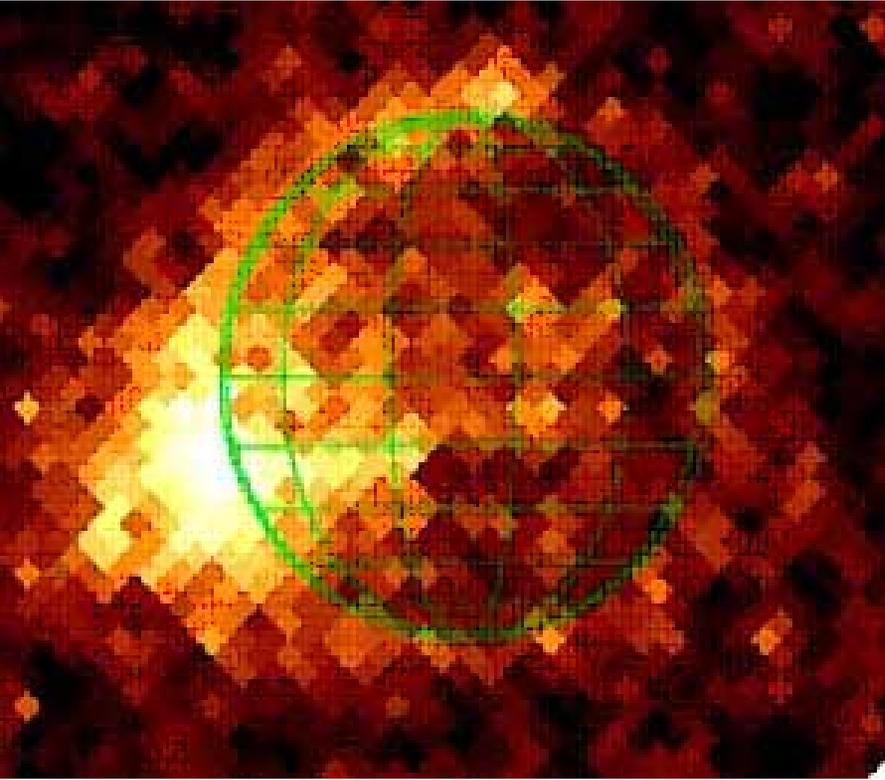
- Volcanic plumes on Jupiter's moon Io are modeled using the direct simulation Monte Carlo (DSMC) method.
- A sophisticated model including - spherical geometry, variable gravity, internal energy exchange (discrete vibration-translation and continuous rotation-translation energy exchange) in the gas, infrared and microwave emission from the gas, multi-domain sequential calculation to resolve the fast emission event and opacity, has been developed.
- Two-phase gas/particle flows are modeled using “overlay” techniques.
- Vent conditions are constrained. Observed plume image, plume shadow, deposition pattern are for the first time reasonably matched with the simulated plumes.

# Modeling Io's Aurora



Geissler 1999, Science 285.

# HST Io Auroral Observation



Trauger *et al.* 1997DPS29.1802T

- Plasma flows right to left
- Image is of [OI] 630nm emission
- Wake bright spot is tilted relative to Io's equator and extends ~250km high
- Little upstream emission
- Bright "equatorial band"
- Limb glow extends from the wake spot to the north polar region
- Diffuse emission present

# Io Auroral Observation II



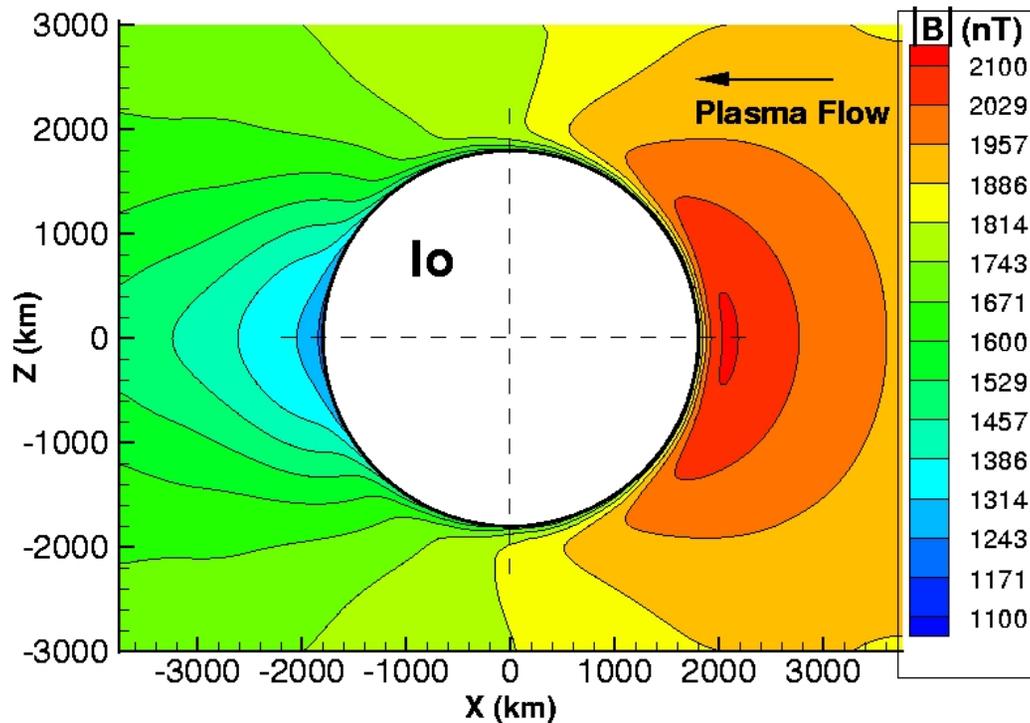
**Cassini movie of emission around Io in eclipse (Porco *et al.*, 2003)**

- During Cassini flyby of Jupiter, several images of Io's emissions were taken
- White spot is Pele
- UV emission shown as blue
- Atomic Oxygen emission (630 nm) is red
- Showed temporal variability of emission
  - Io starts below plasma torus equator and crosses it as the eclipse progresses
  - Emission bright spots appear to track magnetic field tilt



# Magnetic Field Model

- Pre-computed 3D MHD model for Io located at the plasma torus equator (Combi 1998)
  - Includes ion mass loading and no intrinsic field for Io
  - Matched free parameters for best agreement with Galileo flyby data
  - Can get magnetic field at different torus latitudes by rotation
- The field increases ( $\sim 15\%$ ) upstream and decreases ( $\sim 25\%$ ) downstream



# Motion in a Magnetic Field

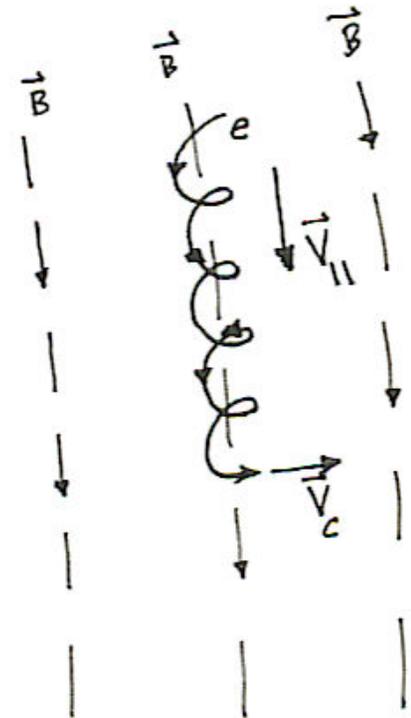
- Convenient to divide electron velocity into components perpendicular and parallel to the magnetic field:

$$\vec{v}_e = \vec{v}_\perp + \vec{v}_\parallel, \quad \vec{v}_\perp = \vec{v}_c + \frac{\vec{E} \times \vec{B}}{B^2}$$

$\vec{v}_c$  = Gyration velocity about field lines

$\frac{\vec{E} \times \vec{B}}{B^2}$  = Drift velocity due to electric field

- We neglect the drift velocity (small compared to  $\vec{v}_\parallel$ ) and diffusion across field lines (collision frequency small)
- The radius of gyration,  $r_g = v_\perp m_e / qB$ , is  $< 6$  m for  $E_e > 5$  eV, and the relevant atmospheric scale is  $\sim 8$  km, so we move the electron purely along the field lines



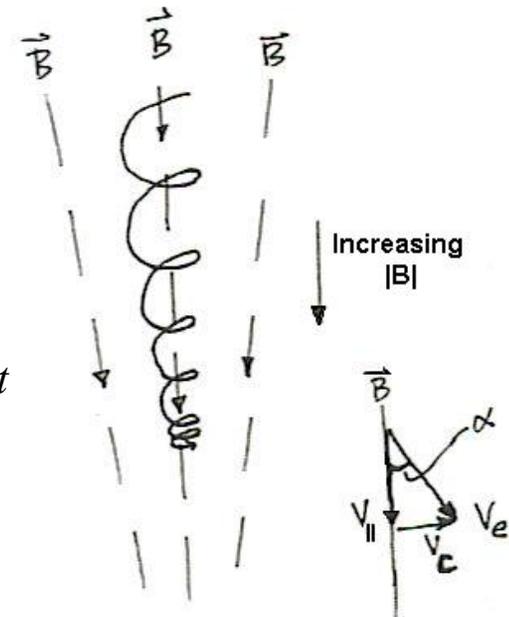
# Magnetic Moment

- An adiabatic invariant for a given electron is:  $\mu_{mag} = \frac{1/2 m_e v_c^2}{|\vec{B}|}$
- Since this is constant along the electron path, a relation for the change in velocity with changing magnetic field strength along a field line can be obtained:

$$\sin \alpha = \sin \alpha_0 \sqrt{\frac{|\vec{B}|}{|\vec{B}_0|}}, \quad \tan \alpha = \frac{\bar{v}_c}{\bar{v}_{\parallel}}, \quad \bar{v}_c^2 + \bar{v}_{\parallel}^2 = const$$

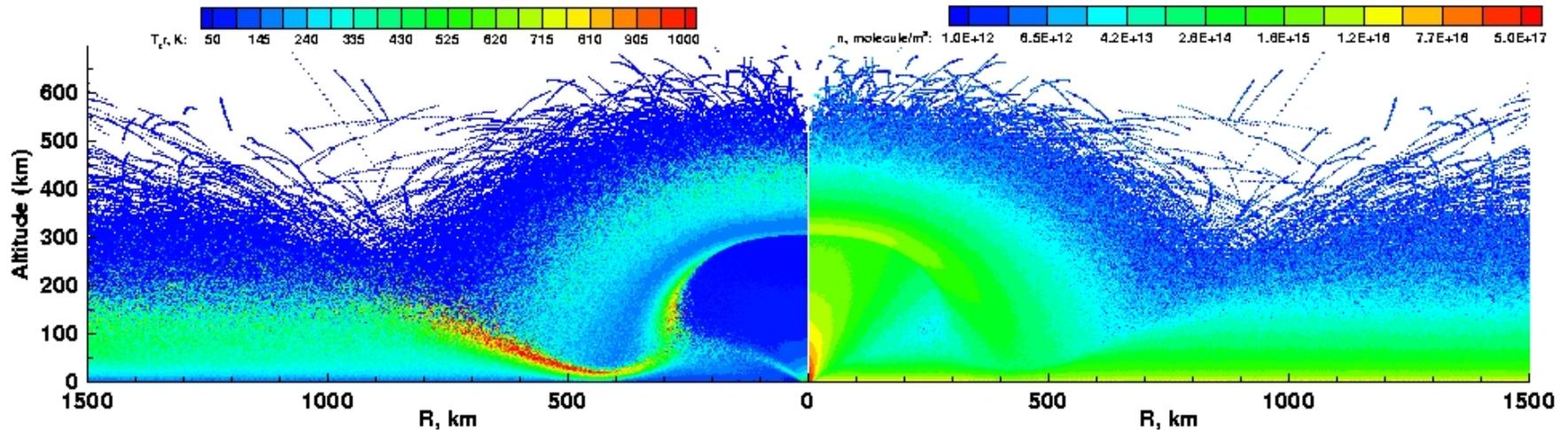
- Note that  $\alpha=90^\circ$  corresponds to  $\bar{v}_{\parallel} = 0$  and that the electron will then reflect (mirror) the electron at:

$$|\vec{B}_{mirror}| = \frac{|\vec{B}_0|}{\sin^2 \alpha_0}$$



# Volcanic Atmosphere Model

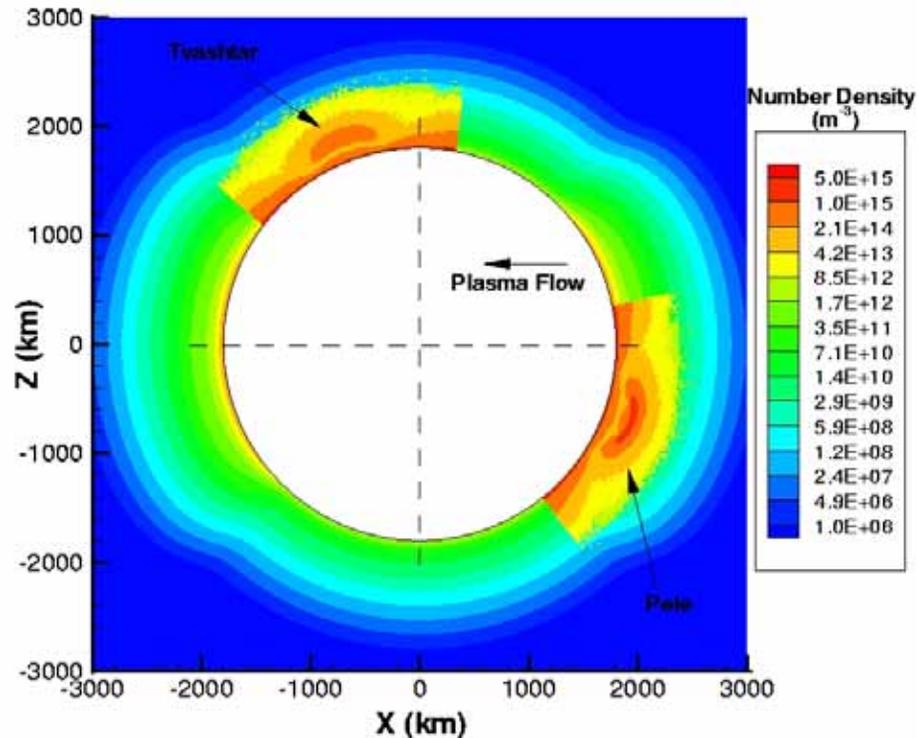
- Pre-computed independent volcanoes (Zhang 2004)
  - Two “template” volcanic types – Large (Pele) and Small (Prometheus)
  - 53 volcanoes accounted for on Io
  - Assume 0.1% O concentration (by number) based on equilibrium vent species’ concentrations computed by Zolotov and Fegley (1998)
  - Plasma heated with energy flux of 5 mW/m<sup>2</sup>



# Sublimation Atmosphere Model

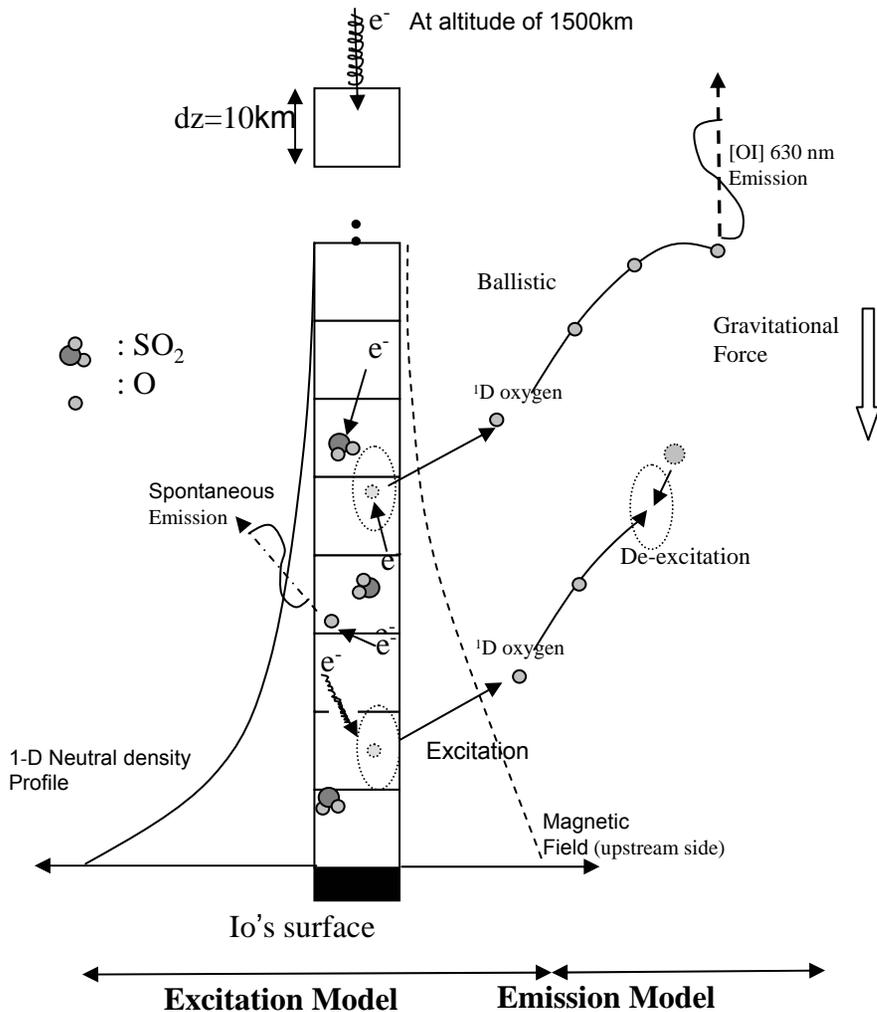
- Pre-computed 2D steady state sublimation atmosphere (Wong 2000)
  - Continuum model – has limited applicability at high altitudes but it is the best available
  - Multi-species model, we use just the SO<sub>2</sub> and O data since they are dominant
  - Atmosphere model for Io in sunlight (not eclipse)
  - Includes photoreactions, plasma reactions
  - Latitudinal dependence added using (Strobel and Wolven) :

$$\frac{n(\theta)}{n_{Pole}} = 1 + \frac{n_{Equator}}{n_{Pole}} e^{\left[-\frac{\theta}{0.625}\right]^6}$$



**Local SO<sub>2</sub> number density profile as viewed from earth (Y = 300km). Notice the latitudinal variation and the superposition of the plumes.**

# Simulation Overview

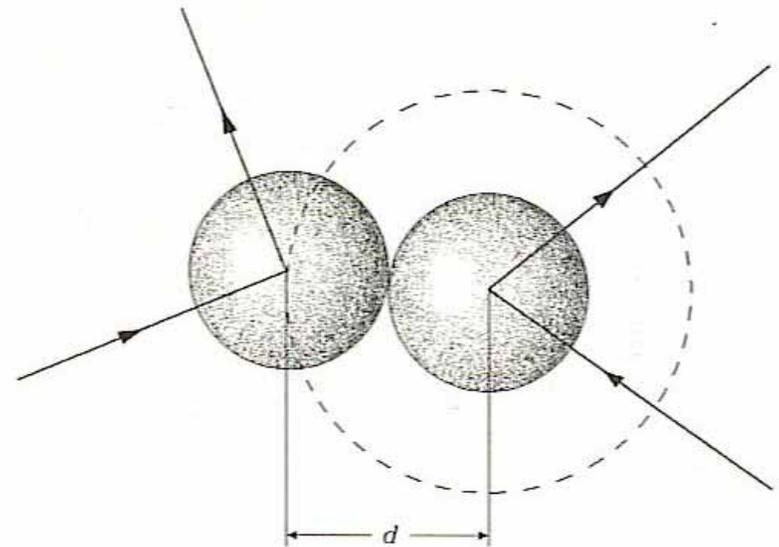


- Model split into two independent parts: Excitation and Emission
- Excitation:
  - Electrons input and move along field lines through the domain
  - Occasionally electrons collide with the neutral atmosphere
  - Location of excited oxygen is stored for use in Emission
- Emission:
  - Excited oxygen are given initial velocities based on local temperature and bulk velocity
  - The oxygen moves until it either collides or emits

# Cross Sections

- A cross section is a measure of the effective area of a target molecule for producing an interaction (collision)
  - Possible interaction types: Ionization, Dissociation, Attachment, Excitation, etc.
- The total cross section for species *i* colliding with *j* is:

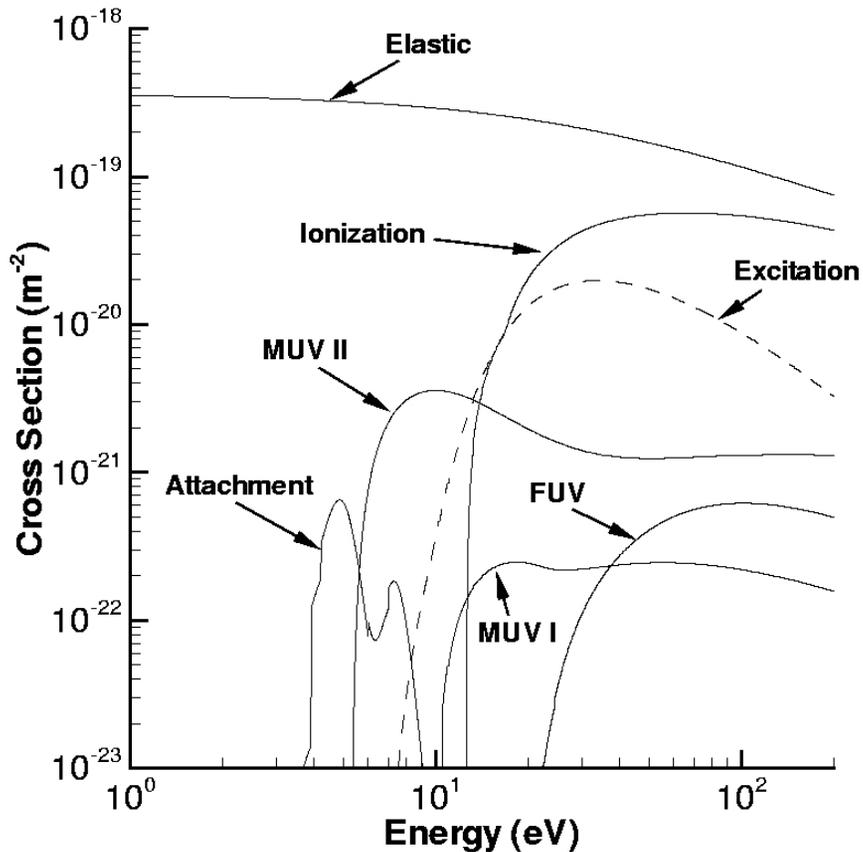
$$\sigma_{ij}^{tot}(E) = \sum_k^{N_{RxN}} \sigma_{ij}^k(E)$$



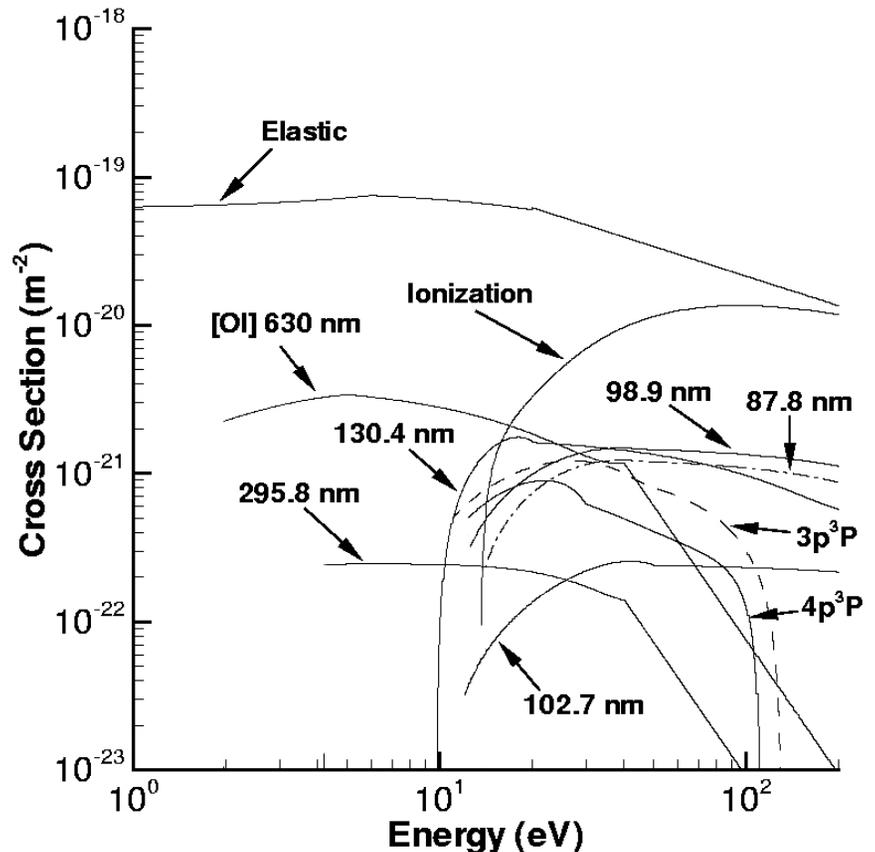
**Hard sphere collision (Bird 1994)**

# Included Cross Sections

The simulation includes electron-SO<sub>2</sub> and electron-O interaction cross sections as functions of energy



SO<sub>2</sub> cross sections



O cross sections

# Collisions

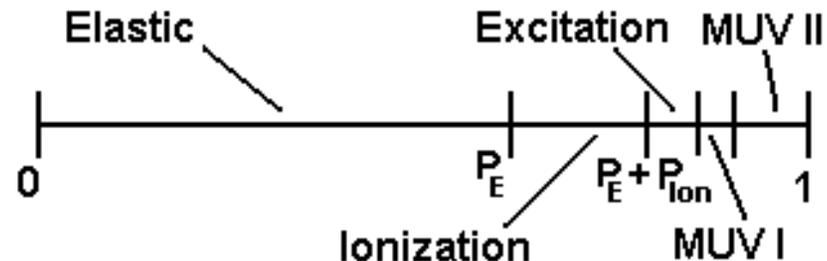
- In a time interval  $\Delta t$ , the collision probability is:

$$P_{Collision} \approx 1 - e^{\left( -\Delta t * \sum_i^{N_s} n_i \bar{\sigma}_{ie}^{tot} \bar{v}_{rel,i} \right)}$$

where  $N_s$  is the number of target species ( $\text{SO}_2$  and  $\text{O}$ ),  $\bar{\sigma}_{ie}^{tot}$  is the total interaction cross section for species  $i$  with the electron, and  $\bar{v}_{r,i}$  is the relative velocity

- A collision occurs if a random number is less than  $P_{Collision}$
- Choose the collision type (elastic, ionization, excitation, etc.) by comparing the position of a second random number on the scale:

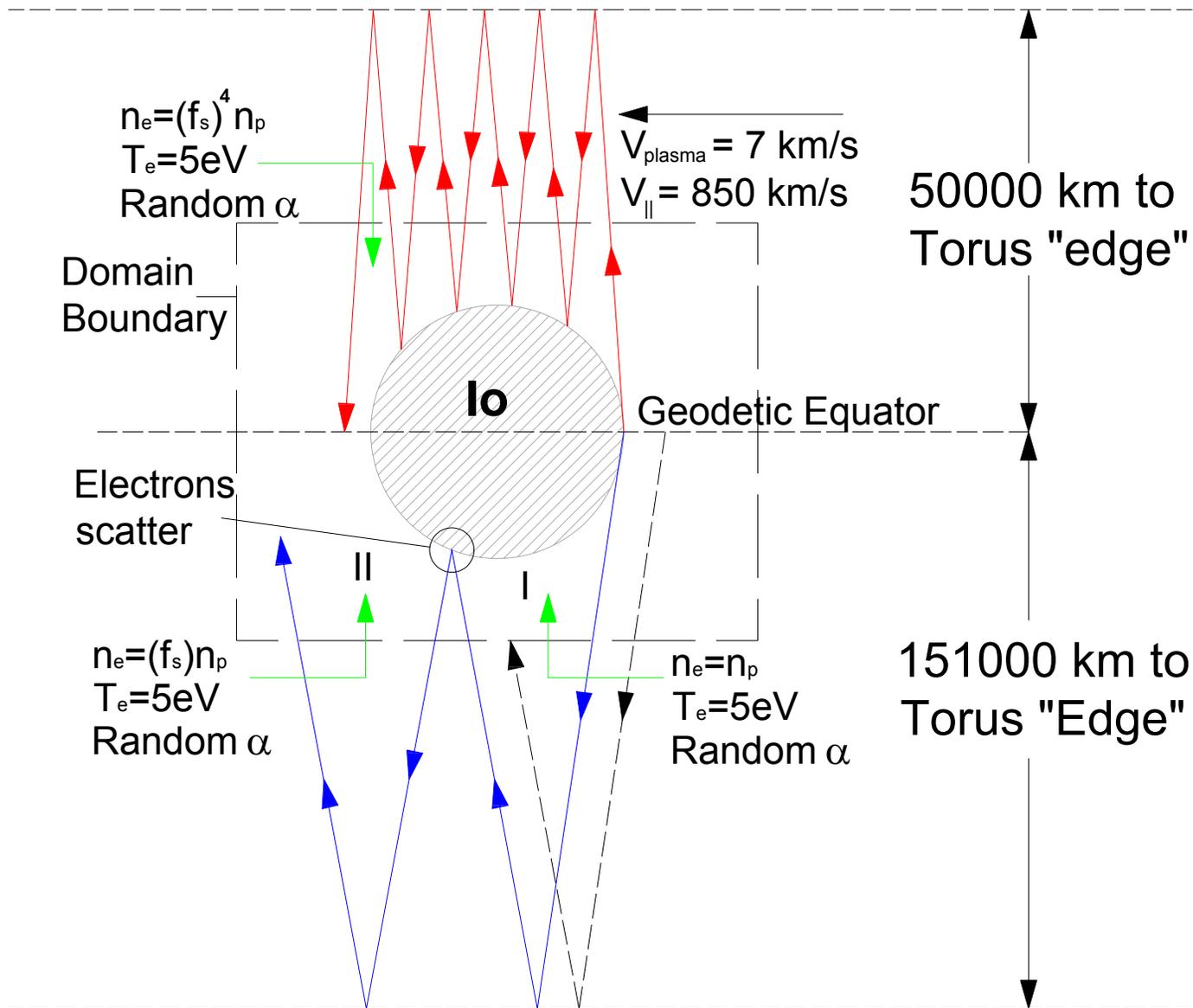
$$P_k(E) = \frac{\sigma_{ie}^k(E)}{\sigma_{ie}^{tot}(E)}$$



# Emission

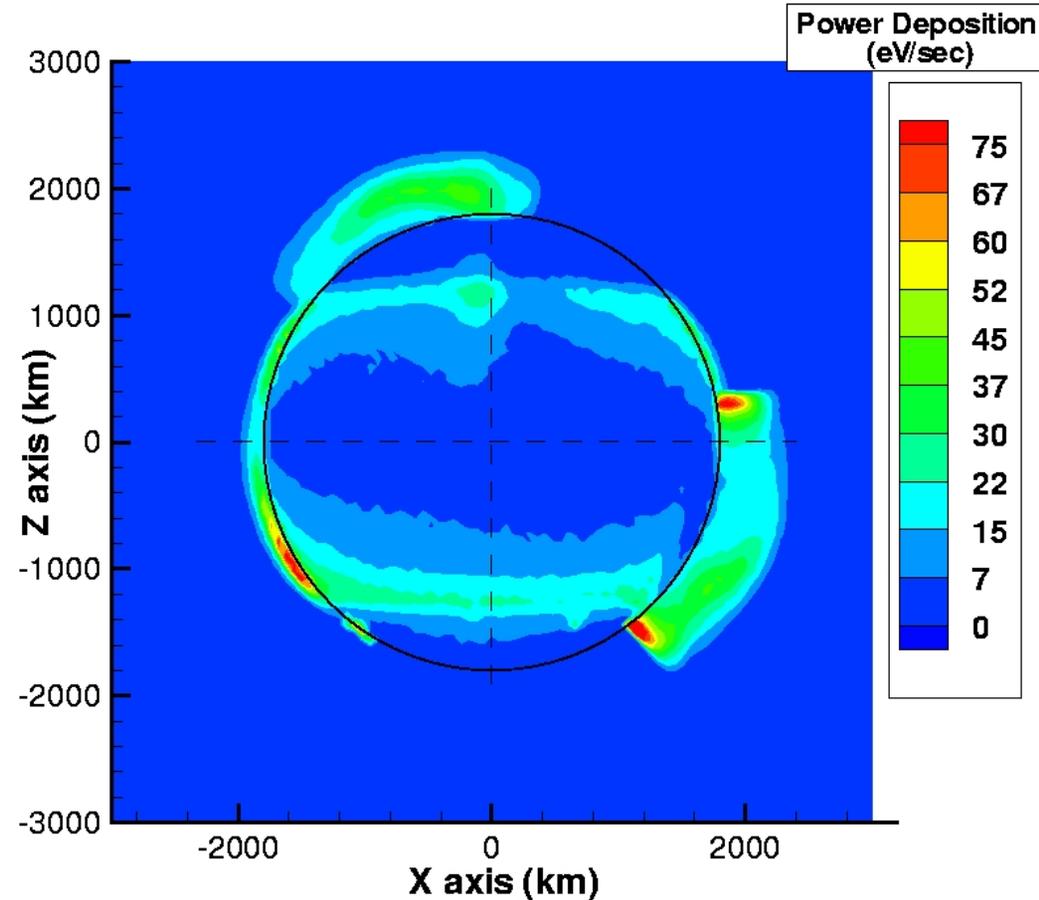
- Excited oxygen given an initial velocity based on local temperature, bulk velocity and corrected for the electron excitation collision
- The rate of emission is given by the Einstein A coefficient (the inverse of A is the mean lifetime of the state)
- [OI] 630 nm is a ‘forbidden’ line emission – it does not emit through the first-order mode, therefore  $A_{630\text{nm}} \sim 5.1 \times 10^{-3}$  (lifetime  $\sim 190$  sec)
- If a collision occurs before the oxygen atom emits, then it is assumed to de-excite (without emission)
- To match observations, the emission events are line-of-sight integrated

# Boundary Conditions



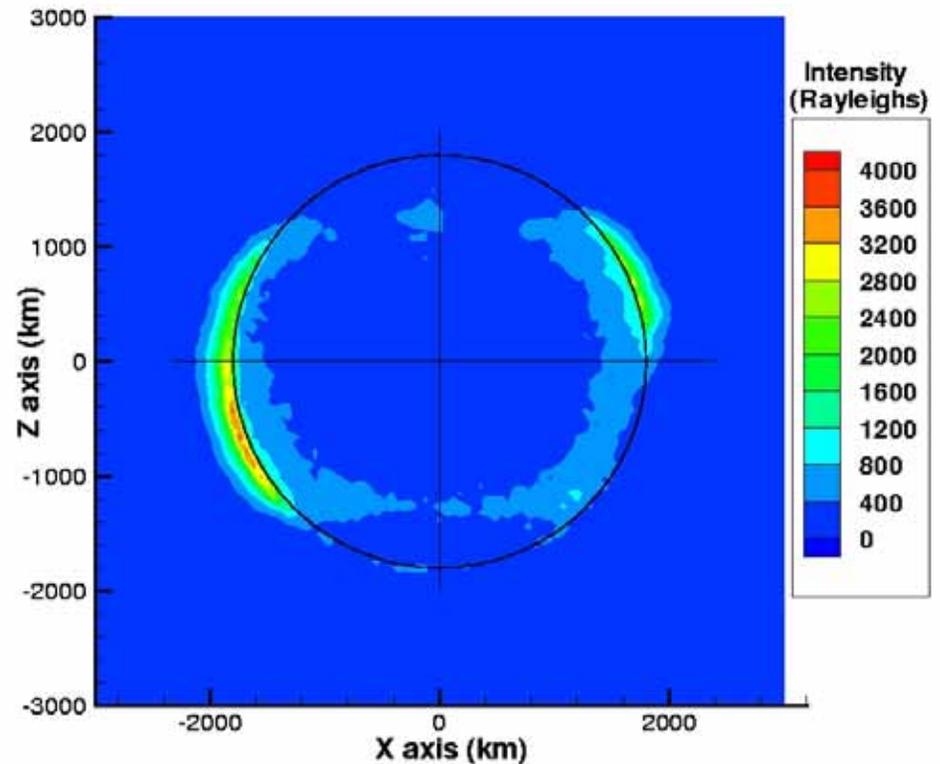
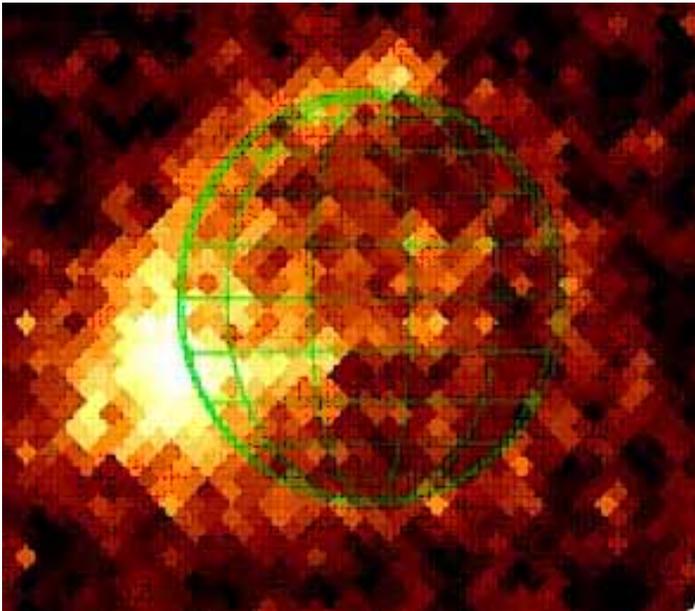
# Auroral Simulation - Deposition

- High electron energy deposition in Pele and Tvashtar
- Higher deposition in the wake than on the upstream side
- Wake deposition is inclined relative to the equator due to electron depletion across Io



# Auroral Simulation – Emission I

- Wake bright spot is tilted relative to Io's equator
- Pele, quenches upstream emission
- No bright equatorial "band" seen in simulation
- Limb glow is not present probably due to Tvashtar and error in latitudinal dependence of atmosphere.



# Conclusions

- Lack of upstream emission due to:
  - Magnetic mirror effect reflecting ~60% of electrons
  - Presence of Pele on the leading edge
- Collisional quenching reduces low altitude and volcanic 630 nm emission
- Asymmetric north/south flux tube depletion results in wake spot tilt – not the magnetic field tilt
- Current Work:
  - Improvements to pre-computed volcanoes
  - Implementing Smyth and Wong's 2004 atmosphere
  - Modeling collapse of dayside atmosphere as eclipse progresses