Seasonal subsurface heat conduction can have a large influence on Triton's \( \text{N}_2 \) frost distribution. Increasing surface thermal inertia reduces the thickness and extent of seasonal \( \text{N}_2 \) frosts. If the thermal inertia of the nonvolatile substrate is greater than about 30% of the value for nonporous \( \text{H}_2\text{O} \) or \( \text{CO}_2 \), or if nonporous \( \text{H}_2\text{O} \) or \( \text{CO}_2 \) is overlaid by a porous regolith of low thermal inertia but less than a few meters thick, the northernmost latitudes visible to Voyager should have been frost-free at the time of the encounter, possibly accounting for their relatively low albedo. If the substrate in the northern hemisphere has sufficiently low albedo and/or emissivity and also has a thermal inertia comparable to that of nonporous \( \text{H}_2\text{O} \) or \( \text{CO}_2 \), there may be no seasonal or permanent \( \text{N}_2 \) deposits toward the poles and very limited seasonal \( \text{N}_2 \) frost in the southern hemisphere at Voyager time, and because of new spectroscopic evidence for nonvolatile \( \text{CO}_2 \) on Triton's bright southern hemisphere, we consider it possible that much of the bright material on Triton's southern hemisphere is \( \text{N}_2 \) frost on Triton.

I.A. Previous Work

The first detailed consideration of frost stability on Triton was by Trafton (1984), who noted that efficient atmospheric transport of latent heat between globally distributed frost patches was likely to equalize global frost temperatures regardless of local insolation. Though Trafton's pre-Voyager model considered \( \text{CH}_4 \) frost, Ingersoll (1990) showed that Voyager observations of Triton's albedo and atmospheric temperature and pressure (e.g., Broadfoot et al. 1989) indicated that Trafton's isothermal frost model was applicable to \( \text{N}_2 \) frost on Triton.

Spencer (1990) constructed a historical model to track long-term trends in \( \text{N}_2 \) frost migration, assuming zero surface thermal inertia, isothermal frost, and Triton's complex seasonal variations in subsolar latitude. The model demonstrated that permanent frost deposits should migrate monotonically to the poles (which are the points of minimum seasonally averaged insolation), and the global equivalent of tens of grams per square centimeter of seasonal deposits should migrate indefinitely between the hemispheres, forming extensive seasonal frost caps in the winter hemisphere. Because the southern hemisphere was experiencing summer at the time of the Voyager encounter, the model predicted the presence there of a relatively small remnant of the previous winter's seasonal cap and extensive frost-free regions. This prediction is in apparent contradiction with the observed brightness of the entire southern hemisphere (McEwen 1990). Similar...
larly, the model predicted tens of grams per square centimeter of fresh seasonal frost extending down to the equator in the northern hemisphere, in apparent contradiction with the relative darkness of the visible northern hemisphere.

Spencer (1990) therefore suggested that fresh frost on Triton might be relatively dark, brightening with time due to insolation, in a manner similar to the Martian polar caps. The dark northern hemisphere seen by Voyager would then be covered by fresh, relatively low-albedo $N_2$ frost, while the southern hemisphere would contain a mixture of bright, nonvolatile substrate and older, brighter $N_2$ frost.

The model also predicted that the atmospheric pressure on Triton should be very unstable, varying by factors of 10 or more, because of the small mass of the atmosphere and its control by the vapor pressure of the surface frosts. Low emissivities, perhaps as low as 0.5, appeared to be necessary to explain the observed atmospheric pressure, given the high albedos derived photometrically from the Voyager data (McEwen 1990, Hillier et al. 1991).

Stansberry et al. (1990) looked in more detail at the albedo patterns seen by Voyager and determined the stability of surface frosts as a function of local albedo and latitude, again assuming instantaneous equilibrium with diurnally averaged sunlight. They reached similar conclusions about the likely current deposition of $N_2$ frost in the visible northern hemisphere and the apparent low emissivity of the $N_2$ frost.

Moore and Spencer (1990) suggested a permanent global asymmetry in the $N_2$ frost distribution on Triton: the Koyaanismuuyaw (Hopi for 'moon out of balance') hypothesis. They suggested that the high albedo of the southern cap might keep it cold enough to be permanently stable, with the thin seasonal northern hemisphere frost remaining dark because it was so transparent that a dark, nonvolatile substrate was visible through it. The widespread presence of probable collapse features in the northern hemisphere led them to suggest that there has been a net nonreversible flux of surface volatiles from the northern to the southern hemisphere over much of the satellite's history.

While Spencer (1990) suggested that much of the bright southern hemisphere of Triton was nonvolatile substrate material with some remnant seasonal frost, Kirk and Brown (1991) offered the alternative that the bright region was largely a permanent cap of solid $N_2$. They suggested that the monotonic poleward shrinkage of the permanent cap predicted by Spencer (1990) was counteracted by viscous spreading of the cap. For instance, a stable cap extending 45° from the pole could thus be maintained if the cap was 1.7 km thick. Brown and Kirk (1991) also showed that internal geophysical heat flow was potentially important in controlling the surface $N_2$ distribution and might provide a positive feedback mechanism that could maintain an inhomogeneous $N_2$ frost distribution.

I.B. Problems to Be Addressed

The work presented here applies a thermophysical historical model to long-term and seasonal volatile migration on Triton. It demonstrates the potential importance of seasonal thermodynamics and shows its influence on frost distribution. In particular, we attempt to address the question of the relative darkness of Triton's northern latitudes and the possibility of a permanent hemispheric asymmetry in the frost distribution.

II. POSSIBLE ROLE OF SEASONAL SUBSURFACE HEAT CONDUCTION

Seasonal surface temperature variations are moderated by the conduction of heat into the subsurface during the summer and its release during the winter. The ability of the surface to store heat is characterized by the thermal inertia, $I$, given by $I = \sqrt{k \rho c}$, where $k$ is the thermal conductivity, $\rho$ is the density, and $c$ is the specific heat. Seasonal heat storage is uniquely important on Triton and Pluto because of their low surface temperatures and the $T^4$ dependence of black body thermal radiation (Sykes et al. 1987, Spencer et al. 1989). The low temperature reduces the efficiency of radiative heat loss during the winter, so more of the heat stored in the subsurface during the previous summer is retained. As a result, temperatures far removed from equilibrium values are possible.

A second factor enhancing the effect of seasonal subsurface heat conduction on Triton is the deep penetration of the seasonal thermal wave into the subsurface, because of the long seasons. The penetration depth $d$ is given by $d = \sqrt{k \tau_s/(2 \pi c)}$, where $\tau_s$ is the seasonal timescale (one Neptune orbital period, 164 years), and thus for constant thermophysical properties will be nine times greater on Neptune than on Mars, for instance. The seasonal thermal wave will thus penetrate into deeper materials that are likely to be less porous and have higher thermal inertia than if the seasons were shorter (see Table I). Though long seasons per se allow temperatures to come closer to equilibrium values, the deep penetration of the thermal wave counteracts this effect if thermal inertia increases with depth.

III. LIKELY SUBSURFACE THERMOPHYSICAL STRUCTURE

III.A. Nonvolatile Substrate

The nonvolatile substrate on Triton, over which the frosts migrate, is likely to consist of $H_2O$, which is proba-
TABLE I

<table>
<thead>
<tr>
<th>Ice</th>
<th>Temperature (K)</th>
<th>(c) (erg g(^{-1}) K(^{-1}))</th>
<th>(k) (erg cm(^{-1}) sec(^{-1}) K(^{-1}))</th>
<th>(\rho) (g cm(^{-3}))</th>
<th>(\Gamma) ((\sqrt{\text{kgpc}})) (erg cm(^{-2}) sec(^{-1/2}) K(^{-1}))</th>
<th>Triton seasonal skindepth (d) ((\sqrt{\text{kgd}(2\pi pc)})) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>H(_2)O</td>
<td>30</td>
<td>(2.3 \times 10^6)</td>
<td>(2.0 \times 10^6)</td>
<td>0.93</td>
<td>(2.1 \times 10^6)</td>
<td>(28,000)</td>
</tr>
<tr>
<td>H(_2)O</td>
<td>40</td>
<td>(3.5 \times 10^6)</td>
<td>(1.5 \times 10^6)</td>
<td>0.93</td>
<td>(2.2 \times 10^6)</td>
<td>(19,000)</td>
</tr>
<tr>
<td>N(_2)(a)</td>
<td>30</td>
<td>(1.2 \times 10^7)</td>
<td>(2.9 \times 10^4)</td>
<td>1.0</td>
<td>(5.9 \times 10^5)</td>
<td>(1,400)</td>
</tr>
<tr>
<td>N(_2)(b)</td>
<td>40</td>
<td>(1.3 \times 10^7)</td>
<td>(2.1 \times 10^4)</td>
<td>1.0</td>
<td>(5.3 \times 10^5)</td>
<td>(1,100)</td>
</tr>
<tr>
<td>CH(_4)</td>
<td>30</td>
<td>(1.5 \times 10^7)</td>
<td>(3.8 \times 10^4)</td>
<td>0.52</td>
<td>(5.4 \times 10^5)</td>
<td>(2,000)</td>
</tr>
<tr>
<td>CH(_4)</td>
<td>40</td>
<td>(1.8 \times 10^7)</td>
<td>(4.2 \times 10^4)</td>
<td>0.52</td>
<td>(6.3 \times 10^5)</td>
<td>(1,800)</td>
</tr>
<tr>
<td>CO(_2)</td>
<td>30</td>
<td>(2.9 \times 10^7)</td>
<td>(4.2 \times 10^4)</td>
<td>1.7</td>
<td>(1.4 \times 10^5)</td>
<td>8,300</td>
</tr>
<tr>
<td>CO(_2)</td>
<td>40</td>
<td>(4.5 \times 10^7)</td>
<td>(2.7 \times 10^3)</td>
<td>1.7</td>
<td>(1.4 \times 10^5)</td>
<td>5,400</td>
</tr>
<tr>
<td>Rhea regolith</td>
<td>(-90)</td>
<td>(8.3 \times 10^8)</td>
<td>(200)</td>
<td>0.5</td>
<td>(3 \times 10^4)</td>
<td>(3^a)</td>
</tr>
<tr>
<td>Rhea regolith</td>
<td>40</td>
<td>(3.5 \times 10^8)</td>
<td>(600)</td>
<td>0.5</td>
<td>(3 \times 10^4)</td>
<td>(500)</td>
</tr>
</tbody>
</table>

Note. Ice thermal properties are from numerous sources compiled by Croft (manuscript in preparation). Seasonal timescale \(t_s\) used in calculating skindepths is 164 years, Neptune's orbital period. Latent heat of N\(_2\) a\(\rightarrow\)b phase transition = \(8.17 \times 10^7\) erg g\(^{-1}\). The Rhea regolith \(\Gamma\) at 90 K is derived observationally from the subsolar temperature of Rhea, and \(\Gamma(90\ \text{K})\) is derived from this, assuming \(\rho = 0.5\) and the known \(\Gamma(90\ \text{K})\) for water ice. Regolith \(\kappa\) is then assumed to have the same \(T\) dependence as nonporous ice, allowing an estimate of \(\Gamma\) and \(d\) for the Rhea regolith at Triton temperatures.

\(^a\) Diurnal skindepth on Rhea.

By analogy with other solid planetary surfaces, any nonporous substrate on Triton is likely to be overlain with a porous regolith of lower thermal inertia. Rhea, because of its icy surface, high albedo, and relatively low surface temperatures, is the closest analog to Triton for which we have thermophysical data. The thermal inertia of Rhea, as determined from a comparison of its albedo and subsolar temperature, is about \(3 \times 10^4\) erg cm\(^{-2}\) sec\(^{-1/2}\) K\(^{-1}\), a good approximation for nonporous H\(_2\)O or CO\(_2\) ices.

Unlike on Rhea, heat conduction in a porous regolith on Triton will be assisted by conduction by the N\(_2\) atmosphere in the pores. Mendis and Brin (1977) give an expression (their Eq. (15)) for gaseous heat transport by Knudsen diffusion (mean free path \(>\) pore diameter) in a porous regolith. Gas conductivity is proportional to mean regolith pore diameter, which is of course unknown, but assuming N\(_2\) gas in vapor pressure equilibrium at 37.5 K, gas conductivity will dominate over grain-contact conductivity if regolith pores exceed 0.1 mm in diameter. The atmosphere may thus also contribute to increasing Triton's regolith conductivity and thermal inertia above the Rhea value.

In conclusion, we adopt the Rhea value of \(3 \times 10^4\) erg cm\(^{-2}\) sec\(^{-1/2}\) K\(^{-1}\) as a lower limit to the thermal inertia of Triton's surface layers, but expect that the actual value may be much higher.

The thickness of any regolith on Triton is unknown. One constraint is the observed impact crater density, which allows estimation of the thickness of an impact-generated regolith. Strom et al. (1990) showed from the few impact craters visible on the Voyager images that Triton's impact crater density is spatially variable and is less than or equal to that of the lunar maria, which have a regolith thickness of \(\sim\)3–16 m (Quaide and Oberbeck 1968). The likely thickness of an impact regolith on Triton is thus between zero and several meters.

III.B. Seasonal and Permanent Frost

As shown by Spencer (1990) and confirmed by the present work, seasonal N\(_2\) frost deposits on Triton have surface densities up to about 100 g cm\(^{-2}\), or 1 m if the frost is nonporous. Table 1 shows that the seasonal skindepth in solid N\(_2\) is a factor of 10 greater than this, indicating that the seasonal thermal wave will mostly "see through" the seasonal N\(_2\) deposits. The conductivity of porous N\(_2\) frost will be greater than that for solid frost, because of...
extremely efficient latent heat transfer by \( \text{N}_2 \) sublimation and deposition across the pores, so that the insulating effects of porous seasonal frost will be even smaller than those of nonporous frost.

The kinetic heat content of the seasonal frost (as opposed to its latent heat content, which is already included in the thermal model) is also negligible. The time required to change the temperature of a frost layer with surface density \( \rho_s \) by \( \Delta T \), for instance by radiation of heat to space, is of order \( (\Delta T \rho_s c)/(\sigma g T^4) \). For \( \rho_s = 100 \text{ g cm}^{-2} \), \( T = 37 \text{ K} \), the frost can cool by \( \Delta T = 1 \text{ K} \) in approximately \( 3 \times 10^6 \) sec, or 30 days. This timescale is so short compared to the seasonal timescale that the heat capacity of the seasonal frost can also be ignored.

The seasonal model thus ignores the thermophysical effects of the seasonal frost deposits and calculates surface temperatures as though the seasonal frost were not there, except that it includes the very important effects of the frost latent heat of sublimation. Figure 1 provides more direct justification for this assumption by showing that a 1 m overlying layer of material with the properties of solid \( \text{N}_2 \) has little effect on the seasonal temperature variations of nonporous \( \text{H}_2\text{O} \) on Triton.

In regions that are permanently frost covered, where the depth of the \( \text{N}_2 \) deposits is arbitrarily large, the thermal inertia of the surface is assumed to be \( 5 \times 10^5 \text{ erg cm}^{-2} \text{ sec}^{-1/2} \text{ K}^{-1} \), the value for nonporous \( \text{N}_2 \) (Table I).

FIG. 1. Demonstration that the heat capacity and conductivity of seasonal \( \text{N}_2 \) frost has little effect on surface temperatures on Triton. Model surface temperatures at 30° N through a range of Triton seasons are shown for a model consisting of nonporous \( \text{H}_2\text{O} \) overlain by no \( \text{N}_2 \), 100 cm of \( \text{N}_2 \), and an infinite thickness of \( \text{N}_2 \). Equilibrium temperatures, appropriate for a surface with zero thermal inertia, are also shown. \( \text{N}_2 \) sublimation and deposition are switched off in this model so that the thermal effects of subsurface heat flow can be isolated. One hundred centimeters of \( \text{N}_2 \), about the maximum thickness of Triton seasonal frost, has very little effect on surface temperatures.

Another potentially important influence on the \( \text{N}_2 \) surface temperatures is the \( \alpha/\beta \) phase transition, which occurs at a transition temperature, \( T_p \), of 35 K. To investigate its effects we ran several single-latitude thermophysical models, ignoring the thermal effects of frost sublimation but including the phase transition. The phase transition was incorporated into a standard numerical thermophysical model (Spencer et al. 1989) by replacing the thermal energy per unit mass of each subsurface slab, \( E_T = cT \), by the total energy per unit mass \( E = E_T + H_\beta f_\beta \), where \( H_\beta \) is the latent heat of the phase transition (Table I), and \( f_\beta \) is the \( \beta \) phase mass fraction. For \( E < cT_p \), \( T = E/c \) and \( f_\beta = 0 \); for \( E > cT_p + H_\beta \), \( T = (E - H_\beta)/c \) and \( f_\beta = 1 \); and for intermediate values of \( E \), where the phase transition is in progress, \( T = T_p \) and \( f_\beta = (E - cT_p)/H_\beta \).

Figure 2 shows the results of two representative runs. The thermal effect of the phase transition is most pronounced when the mean temperature is near \( T_p \) and the conductivity is high so that the thermal wave propagates deeply and a large volume of \( \text{N}_2 \) is involved in the transition. The phase transition, as expected, moderates the seasonal temperature variations because energy goes into changing the \( \text{N}_2 \) phase rather than changing its temperature. The phase change clearly has a significant influence on surface temperatures in some situations, but because of the added computational burden, and because its effects are smaller than those of unknown factors such as the thermal inertia, we did not incorporate the phase transition into our global seasonal thermal model.

The results presented here also do not include the effects of geothermal heat flow from Triton's interior, which has a significant effect on surface temperatures (Brown and Kirk 1991). We have included geothermal heat in several test runs by increasing the temperature at the base of the model at each latitude so that each latitude has a net seasonally averaged heat loss of 6 erg cm\(^{-2}\) sec\(^{-1/2}\), a reasonable value for Triton's geothermal flux (Hansen and Paige 1992). Geothermal heat increases the temperature of unit-emissivity surfaces by about 0.5 K, and the temperature increase should be inversely proportional to the emissivity. Because the effective albedos in the models presented here (Table II) have been adjusted to yield frost temperatures roughly consistent with the Voyager atmospheric pressure, the main effect of including geothermal heat in the model would be to increase the effective albedos slightly, to counteract the expected 0.5–1.0 K surface temperature increase generated by the geothermal heat.

We also do not consider the heating of the atmosphere by passage over warm frost-free regions (Stansberry et al. 1992). To first order, this will not affect frost migration...
because it will increase atmospheric temperature without greatly changing atmospheric density. It is the density that is the dominant control on frost sublimation and deposition rates, because the flux of molecules onto the surface is proportional to \( nV \), where \( n \) is the number density. The dependence on temperature \( T \) is less important because fractional variations in temperature \( T \) are much smaller than fractional variations in \( n \), due to the strong dependence of vapor pressure on temperature.

### V. MODEL DESCRIPTION

The numerical model is based on that described in Spencer (1990) but includes several extra features. Most importantly, subsurface heat conduction is added to the calculation of surface temperatures. Triton's surface is divided into latitude bands, usually with 5° resolution, and for each band temperature is determined as a function of depth and time, and \( N \), frost thickness is calculated as a function of time. A similar thermophysical model has been developed by Hansen and Paige (1992), though their model has higher time resolution (including diurnal effects) but shorter duration and uses different ranges of input parameters.

For areas that are frost free, temperature calculation is essentially identical to that in the conventional thermophysical model described in the Appendix of Spencer et al. (1989), except that two-layer models are possible, with an upper layer of different thermophysical characteristics from the substrate. In one-layer models the only important thermophysical parameter is the thermal inertia \( \Gamma \), but in the two-layer models there are three free thermophysical parameters: the thermal inertias of the two layers and the heat capacity per unit area of the upper layer, \( C \), given by \( C = \rho c t \), where \( t \) is the layer thickness. The upper layer was normally divided into just three slabs in the numerical model: test runs with higher depth resolution had very similar surface temperatures. Thermophysical properties were assumed to be temperature independent.

For frost-covered regions, we assume, as in Spencer (1990), that all frost has the same surface temperature because of efficient transport of latent heat in the atmosphere (Trafton 1984). Frost surface temperature \( T_F \) at each timestep was thus calculated for all frost simultaneously by balancing integrated insolation and heat conduction from the subsurface against thermal radiation into space:

\[
\int_a k \left( \frac{\partial T}{\partial x} \right)_{x=0} da + \int_a (1 - A)S da - \omega a T_F^4 \quad (1)
\]

Here \( \int_a da \) denotes integration with respect to area over the entire frost-covered surface, \( a \) is the total frost-
covered surface area. $x$ is the depth into the subsurface. $T$ is the temperature, which is a function of latitude, time, and depth $x$. $A$ is the bolometric albedo. $S$ is the local insolation, and $\varepsilon$ is the emissivity.

We then calculate subsurface temperatures in the frosted regions using the same standard thermophysical model as that in the frost-free regions. We determined the local frost sublimation or deposition rate using the local balance between insolation, conduction, radiation, and latent heat transfer,

$$k \left( \frac{\partial T}{\partial x} \right)_{x=0} + (1 - A)S + L \dot{m} = \varepsilon \sigma T_\text{eq}^4,$$

(2)

where $I$ is the latent heat of sublimation of $N_2$ frost and $\dot{m}$ is the local rate of frost deposition.

Differing albedos for the frosted and frost-free regions can be specified. Because the emissivities of the surface materials are unknown we used the “effective albedo” $A'$, given by $(1 - A') = (1 - A)/\varepsilon$, as in Spencer (1990), as a measure of the albedo. Equation (2) now becomes

$$k' \left( \frac{\partial T}{\partial x} \right)_{x=0} + (1 - A')S + L \dot{m}' = \varepsilon \sigma T_\text{eq}^4.$$

(3)

where $k' = k/\varepsilon$ and $\dot{m}' = \dot{m}/\varepsilon$. Actual thermal conductivities and frost thicknesses are thus smaller than the model values $k'$ and $m'$ by the factor $\varepsilon$.

As in the model of Spencer (1990), calculation of temperatures and frost deposition and sublimation rates is continued for long periods (up to 40,000 years) with various initial frost distributions. If sustained sublimation reduces the local frost thickness to zero, that latitude is considered frost-free and the surface temperature is then calculated using the standard thermophysical model. Conversely, if the temperature of a frost-free latitude drops below the current atmospheric temperature, then frost deposition starts at that latitude, and its temperature is determined by Eq. (1). Because the temperature of the lowest slab of the thermal model (which is held constant during each run) has a significant effect on the surface temperatures and frost distribution, this was adjusted iteratively with multiple runs of the model (typically five runs). The base temperature at each latitude was set equal to the seasonally averaged surface temperature at that latitude in the previous run. The globally and seasonally averaged thermal balance of the model (ratio of total insolation to total thermal emission) improved with each run and by the final run mean insolation and emission were typically balanced to better than 1 part in $10^4$. Our 1990 model showed that a global average of no more than about 20 g cm$^{-2}$ of $N_2$ frost migrated seasonally, so the present model used a global frost inventory of 50 g cm$^{-2}$ to ensure full development of seasonal frosts. Excess frost collects at the poles.

An additional option was added to the model in response to the suggestion of Brown and Kirk (1991) and Kirk and Brown (1991) that the secular migration of volatiles to Triton’s poles, mentioned in Section I.A, might be balanced by viscous spreading of the permanent polar caps toward lower latitudes. We simulated such a cap, when desired, by defining the cap to be the region poleward of a specified latitude and redistributing the frost deposits in the cap region as necessary to prevent bare ground from being exposed within the cap boundary. The redistribution conserved the total frost inventory within the cap boundary, which could however change due to normal sublimation processes.

VI. MODEL RESULTS

VI.A. Hemispherically Symmetric Models

A primary motivation for the thermal modeling was to investigate the possibility that frost deposition in the darker northern hemisphere seen by Voyager might be inhibited by the finite thermal inertia of the subsurface, i.e., that the visible regions had not yet cooled off enough from the previous northern summer to develop thick frost deposits. Figure 3 and 4a show results for various substrate thermal inertias, assuming substrate thermal properties constant with depth. Values of $\Gamma > 5 \times 10^6$ erg cm$^{-2}$ sec$^{-1/2}$ K$^{-1}$, well within the range of plausible thermal inertias for Triton, are sufficient to prevent deposition.
THERMAL INERTIA ON TRITON

FIG. 3. Frost thickness (bold contours) and bare ground temperatures (dashed contours) vs time and latitude for two extreme substrate thermal inertias ($I$): $3 \times 10^4$ (a; model A in Table II) and $2 \times 10^6$ erg cm$^{-2}$ sec$^{-1/2}$ K$^{-1}$ (b; model F in Table II). Frost thickness contours are at 1, 3, 10, 30, 100, 300, and 1000 g cm$^{-2}$. a is very similar to models where $I = 0$ is assumed, e.g., Fig. 1. of Spencer (1990), with extensive northern seasonal frosts at the time of the Voyager encounter (dotted vertical line). In b, in contrast, the high thermal inertia suppresses almost all seasonal frost and reduces seasonal temperature variations in the frost-free regions. The curve oscillating about the equator marks the locus of the subsolar point.

of fresh frost in the northernmost regions visible to Voyager at the time of the encounter. Because porosity in nonvolatile substrates will reduce $I$, the thermal inertia of a CH$_4$ substrate could prevent visible northern frost only if it was effectively nonporous (Eluszkiewicz, personal communication), but somewhat porous H$_2$O and CO$_2$ substrates are consistent with the lack of visible northern frost (Table I). These runs require an effective bolometric frost albedo of 0.65 to maintain the observed atmospheric pressure, lower than photometric estimates of Triton's southern hemisphere albedo. The discrepancy, similar to that found in the simpler models of Spencer (1990) and Stansberry et al. (1990), may indicate a low emissivity for the N$_2$ frost on Triton. Including geothermal heat in the model would reduce the discrepancy and increase the inferred emissivity slightly (Section IV).

Figure 4b shows a similar plot for two-layer thermophysical models, in which a lower semi-infinite layer $I = 2 \times 10^6$ erg cm$^{-2}$ sec$^{-1/2}$ K$^{-1}$, appropriate for nonporous H$_2$O or CO$_2$, is covered with a variable thickness "regolith" of Rhea-like material ($I = 3 \times 10^4$) or a more conductive regolith ($I = 1 \times 10^6$). Again, as expected, a thinner regolith inhibits frost formation in the northern hemisphere at the time of the Voyager encounter. Model H, with 2 m of regolith that has three times the thermal inertia of Rhea, overlying nonporous H$_2$O or CO$_2$ ice, a very plausible thermophysical structure based on the arguments of Section III A, is frost-free in the northern hemisphere as far north as Voyager could see. An effective albedo of 0.63 is used for the two-layer model to achieve rough consistency with the observed atmospheric pressure, again suggesting a low emissivity for the N$_2$ frost.

All these models suffer from the problem of ever-shrinking permanent polar caps, first encountered by Spencer (1990) and Stansberry et al. (1990). They predict that most

FIG. 4. Frost thickness vs latitude at Voyager encounter time for various thermal models. a shows results of homogeneous substrate models A--F. Low-latitude frost thickness decreases monotonically with increasing $I$, though in the southern hemisphere models E and F coincide. b shows results of two-layer models with substrate $I$ consistent with nonporous H$_2$O or CO$_2$. 

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of Triton's N$_2$ inventory will retreat to the poles, and the southern hemisphere at the time of the Voyager encounter should have been mostly frost-free, with a residual seasonal cap extending no further north than about 45° S.

**VI.B. Koyaanismuyaw Models**

If all the frost is initially placed in the one hemisphere (the southern one, for instance), and the substrate material has sufficiently low albedo and high thermal inertia, then the exposed substrate of the northern hemisphere never cools off enough in the winter to allow a permanent cap to form there. However, the southern cap still shrinks monotonically with time and eventually all but the extreme southern latitudes of Triton are frost-free. If, however, the permanent polar cap is forced to maintain a large size, as by viscous spreading or any other process, it is possible to maintain a frost-covered southern hemisphere and frost-free northern hemisphere indefinitely under some circumstances, as suggested in the Koyaanismuyaw hypothesis of Moore and Spencer (1990). Figure 5a shows an example of this (model L).

Figure 5b shows a rather different model, model O, in which the southern cap is not forced to maintain a fixed size but the substrate in the southern hemisphere of Triton is as bright as the frost ($A' = 0.70$). The northern hemisphere substrate has $A' = 0.50$. Winter seasonal frosts form in the northern hemisphere, as in model L, but, paradoxically, *summer* seasonal frosts form in the south. This is because in this model the permanent cap $\Gamma$ is less than the substrate $\Gamma$ [as is reasonable if the cap is nonporous N$_2$ and the substrate is nonporous H$_2$O or CO$_2$ (Table I)], so during the southern summer the frost temperature increases faster than the temperature of the bright southern hemisphere substrate. When the frost temperature exceeds the nearby substrate temperature, summer frost forms. This model reflects the idea, suggested by Moore and Spencer (1990) and discussed in Section VII.B, that the nonvolatile material in the southern hemisphere may be intrinsically bright.

If even a small permanent cap forms in the northern hemisphere and has the same albedo as the southern cap, the southern cap becomes unstable with respect to the north cap because it extends to lower latitudes and thus has greater mean seasonally averaged insolation. Frost then rapidly transfers to the northern hemisphere until the southern cap shrinks to the size of the northern cap. This severely limits the range of conditions under which the global asymmetry can be maintained, and the allowed range is shown in Fig. 6 for the case of a homogeneous (one-layer) substrate. The models shown in Fig. 6 all have an effective frost albedo of 0.75, which results in an atmospheric pressure consistent with the Voyager observations when the models are stable. Note that the observed atmospheric pressure is achieved with an effective frost albedo higher (and thus a higher emissivity) than that in the hemispherically symmetric case. This is because the lack of a large northern polar cap in the Koyaanismuuayaw models increases the global mean insolation on the frost in 1989, and this increases the frost temperature for a given albedo. Figure 6 shows that unless the Triton's north polar regions are much darker than the regions seen by Voyager or have very low emissivity, a global frost asymmetry can only be maintained if, as is certainly possible, the thermal inertia of the substrate is very close to that for H$_2$O or CO$_2$ ice.

Koyaanismuuayaw models with a two-layer substrate in which the upper "regolith" layer is thin enough to maintain the global frost asymmetry are time-consuming to calculate because extremely high time resolution is required to maintain numerical stability. For this reason, we have not yet explored such models in detail.
VI.C. Atmospheric Stability

Atmospheric pressure as a function of time is obtained from the frost temperature and the N₂ vapor pressure curve (Brown and Ziegler 1980). The timescale \( t_s \) for changing the atmospheric pressure is given by the ratio of its latent heat content to the rate of radiative heat loss; i.e., \( t_s = \frac{Lm}{\sigma T^4} \), where \( m \) is the column density of the atmosphere (Trafton and Stern 1983). For an N₂ atmosphere at 38 K and an emissivity of 0.7, \( t_s = 86 \) days, which is much shorter than the seasonal timescale. We have already shown that the specific heat of the seasonal frost deposits is not a significant factor in moderating surface temperature changes (Fig. 1 and Section III.B). We thus assume that the atmospheric pressure adjusts instantaneously to changes in frost temperature.

The frost migration models of Spencer (1990), which assumed a surface with zero thermal inertia, predicted a very unstable atmospheric pressure and a possible atmospheric collapse within the next decade as the remains of the previous winter’s seasonal cap sublimated away during the southern summer. Including a finite thermal inertia moderates these changes somewhat and may even result in a pressure increase in the coming decade, but large atmospheric pressure variations still occur, as shown in Fig. 7.

High-thermal-inertia substrate models have increasing atmospheric pressure at present because insolation is increasing on the southern cap and there is little northern seasonal frost to radiate the heat away (remember that frost temperature is determined by the mean insolation on all surface frosts). Low-thermal-inertia substrate models, with extensive seasonal frost deposits, have currently decreasing atmospheric pressure because of the decreasing area of sunlit southern seasonal frost and the large area of shadowed northern seasonal frost. Koyaanismuuyaw models, with no permanent northern cap at all, show the most extreme pressure variations because during northern summer almost all the surface N₂ frost is in darkness. Triton’s atmospheric pressure can occasionally be monitored from Earth by means of stellar occultations, so there is a chance to distinguish observationally between these models in years to come.

As in Spencer (1990), the model implicitly assumes that the atmospheric pressure is always above about 1 μbar. At lower pressures winds due to volatile migration become supersonic and the condition of isothermality inherent in the model ceases to apply. However, the only models with extensive periods of submicrobar atmospheric pressure are the Koyaanismuuyaw ones, and in these there is negligible frost migration anyway, so the low pressures do not invalidate these models.

VII. DISCUSSION

VII.A. Northern Hemisphere

We have demonstrated that seasonal subsurface heat storage, with reasonable assumptions about surface structure, can prevent or greatly reduce frost deposition in visible northern latitudes at the time of the Voyager encounter and thus provides a plausible explanation for the relative darkness of this part of Triton. Recent work by Lee et al. (1992) has shown that the dark regions of the northern hemisphere are anomalously forward-scattering, which may indicate the presence of a thin, relatively transparent layer of fresh frost, and Eluszkiewicz (1991) has shown how such a layer might form in N₂ frost. The equilibrium model of Spencer (1990) predicted 20–30 g cm⁻² of N₂ frost in this region, but the current model allows much thinner frost deposits in the visible northern hemisphere, which might be more easily made transparent. However, if the anomalously scattering region is indeed covered by a transparent frost layer, the thermal inertia in this region must be small enough to allow at least some frost deposition.

Yelle (1992) suggested another explanation for the relative darkness of Triton’s northern hemisphere: that frost is deposited preferentially in colder shaded regions where it is less visible. This mechanism could work in conjunction with the finite thermal inertia to reduce the visibility of frost deposits in this region.

The suggestion of Spencer (1990) that fresh N₂ frost on Triton might be relatively dark is not directly addressed by the new models. This remains a possible explanation...
VII.B. Southern Hemisphere

We have not solved the problem of the apparent large extent of the bright material in the southern hemisphere if this material is predominantly \( \text{N}_2 \), because secular poleward migration of the permanent polar caps occurs in the thermophysical models as in earlier equilibrium models, and seasonal frosts are not very extensive in the southern hemisphere at the time of the Voyager encounter in any of our models. The viscous spreading model of Brown and Kirk (1991) and Kirk and Brown (1991) provides a mechanism for maintaining a large southern cap of bright \( \text{N}_2 \), but only if all permanent low-latitude \( \text{N}_2 \) deposits are physically connected by flowing "glaciers" to deposits at much higher latitudes. The presence of isolated low latitude high-albedo patches, such as the aureoles of the "mushrooms" at approx. 20° S, 60° E (Fig. 30 of Smith et al., 1989), is difficult to explain by this mechanism, and if this bright material is not \( \text{N}_2 \), it is plausible that much of the rest of the bright material in the contiguous bright regions is not \( \text{N}_2 \) either. Also, the visibility of the global linear ridge network in the extreme southern latitudes implies that any frost deposit is probably less than 1 km thick.

Recent spectroscopic observations by Cruikshank et al. (1991 and personal communications) show the presence of \( \text{CO}_2 \) on Triton's surface. The depth of the deepest \( \text{CO}_2 \) features is about 10%, comparable to the depth of \( \text{CO}_2 \) absorptions on the Martian \( \text{CO}_2 \) polar cap. The minimum areal coverage of \( \text{CO}_2 \)-containing material on Triton, if the intrinsic depth of the bands in pure \( \text{CO}_2 \) was 100%, is thus 0.01% of the projected disk (weighted by the continuum albedo at 8 μm). However, if the Martian cap spectrum is a good analog, the intrinsic depth of the \( \text{CO}_2 \) features may be much less than 100%, and the areal coverage on Triton correspondingly much greater. Because only 12% of Triton's projected disk was occupied by the northern hemisphere at the time of the observations, it is quite likely that a considerable fraction of the southern hemisphere is occupied by \( \text{CO}_2 \), a nonvolatile material at Triton temperatures. These observations thus lend support to the idea that at least some of the bright material in the southern hemisphere is nonvolatile substrate rather than \( \text{N}_2 \) frost. As mentioned by Spencer (1990), the strong \( \text{CH}_4 \) absorptions in Triton's spectrum (Cruikshank et al. 1988,
Spencer et al. 1990, Grundy and Fink 1992) also provide evidence for extensive nonvolatile exposure in the southern hemisphere, because although CH₄ is somewhat volatile, its surface abundance is probably greater than its atmospheric abundance. However, if much of the exposed bright southern material is nonvolatile, its high albedo in the presence of possible dark airborne particulates from the plumes (Soderblom et al. 1990) may require a cleaning mechanism. Possibilities include the removal of dark particles by wind (Sagan and Chyba 1990), especially during periods of high atmospheric pressure, or endogenic resurfacing.

Yelle (1992) argues that the westward winds at 10 km altitude at 50° S latitude, revealed by the active plumes there, require that the equatorial regions be warm and probably frost-free. However, it is also possible that the warmer frost-free regions are part of the bright southern hemisphere materials: warm frost-free regions anywhere northward of 50° S could explain the wind directions at the latitude of the plumes.

Moore and Spencer (1990) noted that the bright southern hemisphere material has appreciable thickness (>~10 m) and discrete boundaries and occupies low-lying areas, which is consistent with a material endogenically emplaced. Thus the hemispheric asymmetry of Triton may be analogous to that of Mars, whose northern half has been resurfaced by endogenic materials.

Here we suggest that these arguments and the model presented here provide additional evidence that much of Triton's bright southern hemisphere is high-albedo nonvolatile material, probably with intermixed permanent and remnant seasonal N₂ frost, as suggested by Spencer (1990). The gross hemispheric albedo asymmetry may be due to the difference in the intrinsic albedos of endogenically emplaced refractory materials composing the sub- strate and not be dependent on the precipitation of volatiles. Model O (Fig. 5b) shows that summer seasonal frosts may occur if there is high-albedo nonvolatile material in the southern hemisphere. It is even possible that the appearance of a southern hemisphere summer frost, covering previously exposed UV-dark material, contributed to the remarkable apparent increase in Triton's UV albedo and possible decrease in CH₄ absorption strength during the 1980s (Cruikshank et al. 1988, Smith et al. 1989, McEwen 1990, Pollack et al. 1990).

VII.C. Permanent Hemispheric Asymmetries

Models L–O presented here show that it is possible for almost all the N₂ frost to remain permanently in the southern hemisphere, but only if the northern hemisphere has a low effective albedo and high thermal inertia. In this case the effective albedo (and thus the emissivity) of the N₂ frost is higher than that in the hemispherically symmet-


